

# From Neutrino Factory to Muon Collider



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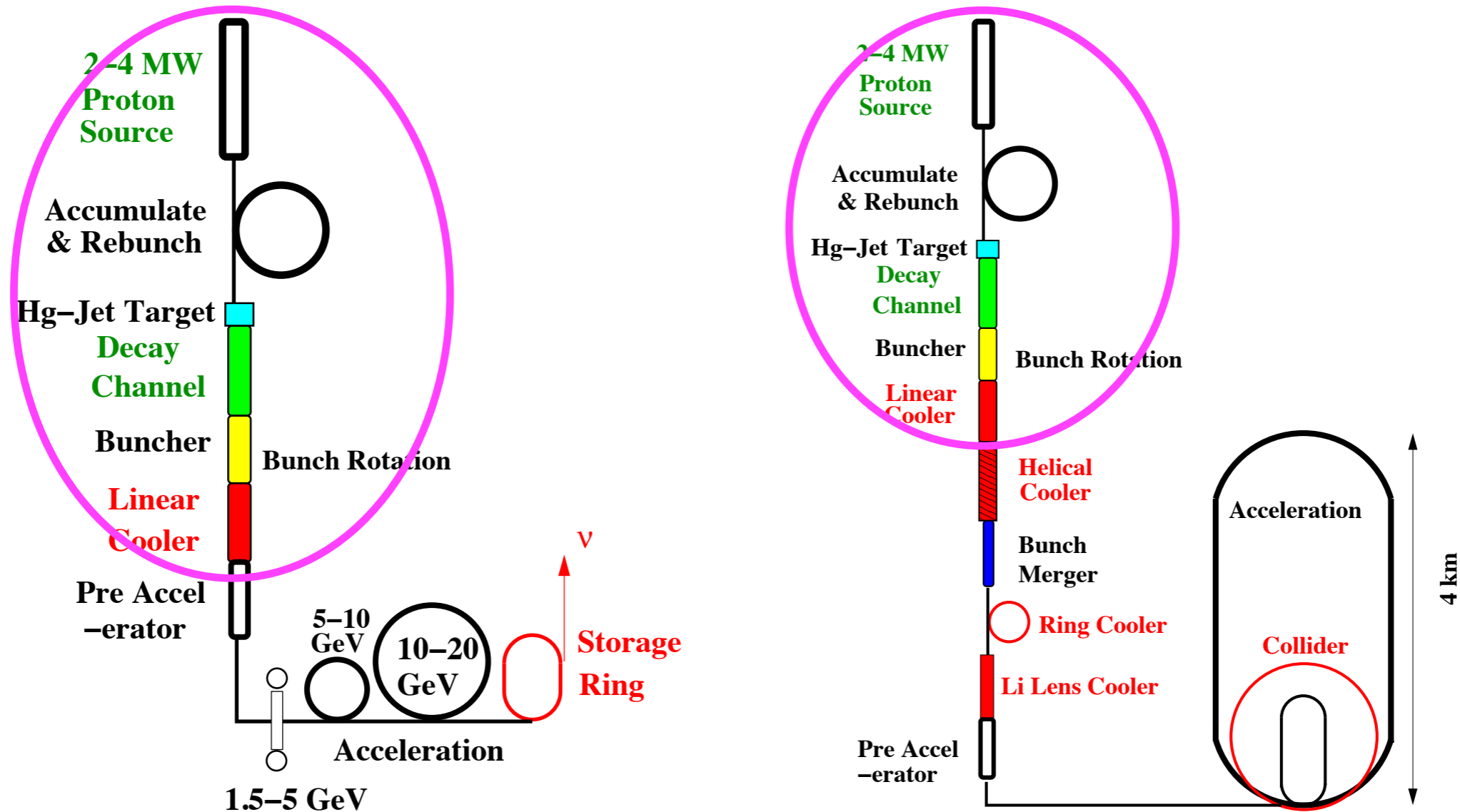


NuFact'10  
Tata Institute of Fundamental Research  
Mumbai, India  
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# Outline

- Neutrino Factory/Muon Collider Comparison
- Muon cooling for a Neutrino Factory or Muon Collider
- 6D cooling
- Final cooling
- Acceleration
- Storage ring
- Conclusions

# $\mu$ C-vF Comparison



● Front ends similar or identical!

➔ Can  $\mu$ C be built as vF upgrade?

# Key $\mu\text{C}$ Parameters

Table 2. Example parameters for a 1.5 TeV (c.m.) muon collider [26].

	LEMC	HEMC
Avg. luminosity ( $10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ )	2.7	1
Avg. bending field (T)	10	8
Proton driver repetition rate (Hz)	65	15
$\beta^*$ (cm)	0.5	1
Muons per bunch ( $10^{11}$ )	1	20
Muon bunches in collider (each sign)	10	1
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Norm. Long. Emittance (m)	0.35	0.07
Energy spread (%)	1	0.1

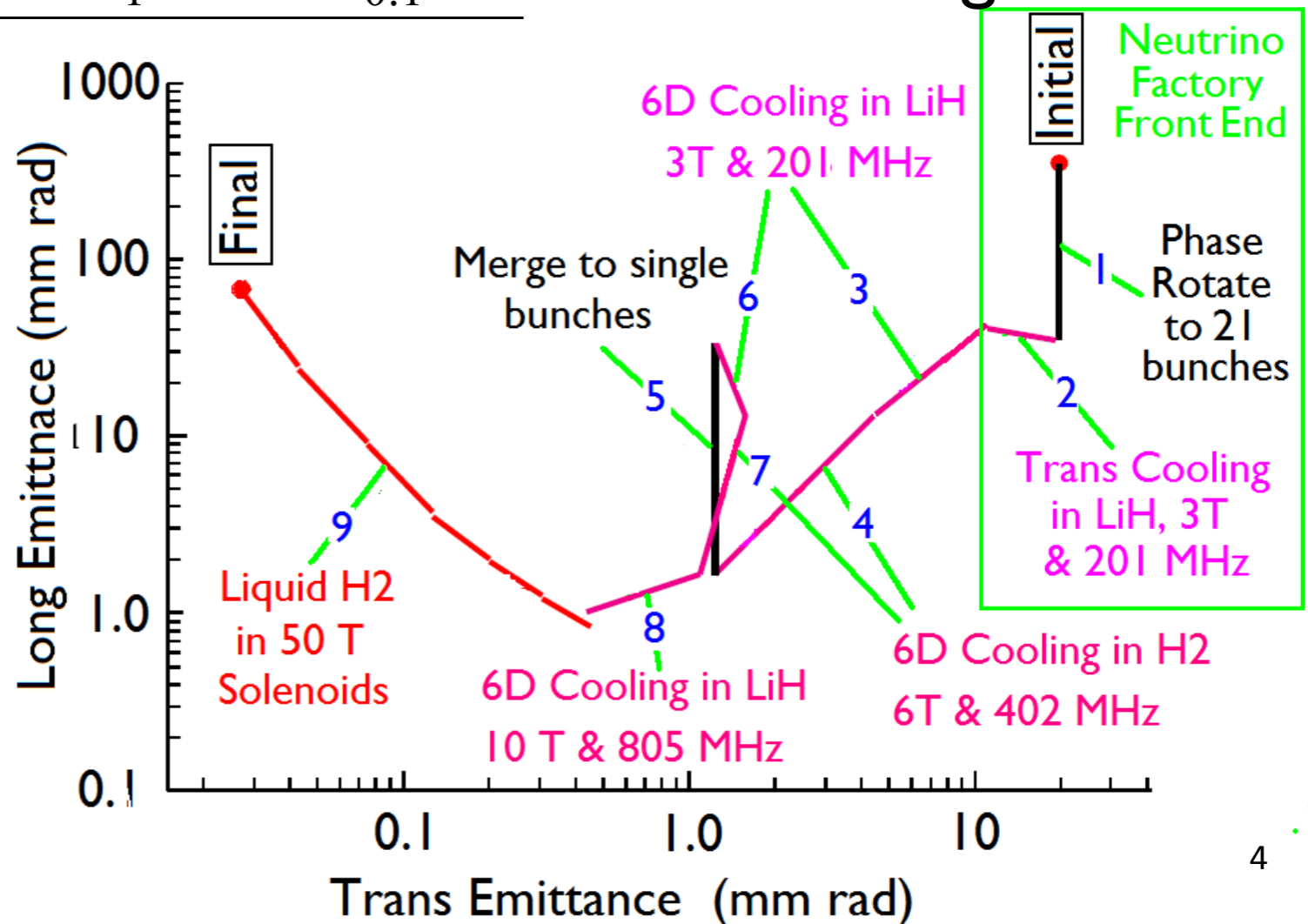
● 2 ways to get  $10^{34}$

● compare with  $\nu\text{F}$ :

7,400 Need  $\sim 300\text{X}$  more cooling than  $\nu\text{F}$ !

● How to get there:  
(1 scenario)

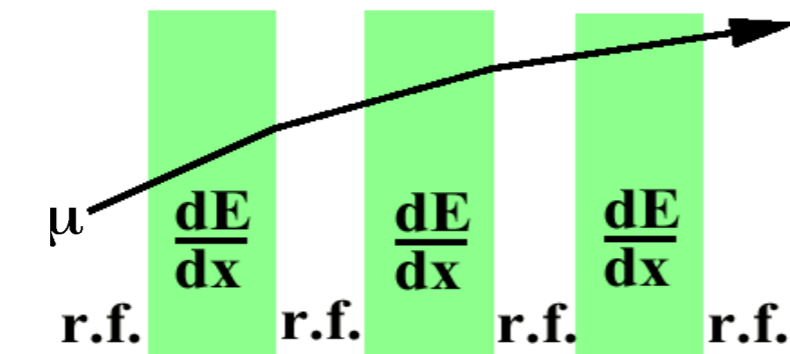
● Must cool both transversely and longitudinally



# Ionization Cooling

Reminder:

- Muons cool via  $dE/dx$  in low- $Z$  medium:



– Absorbers:

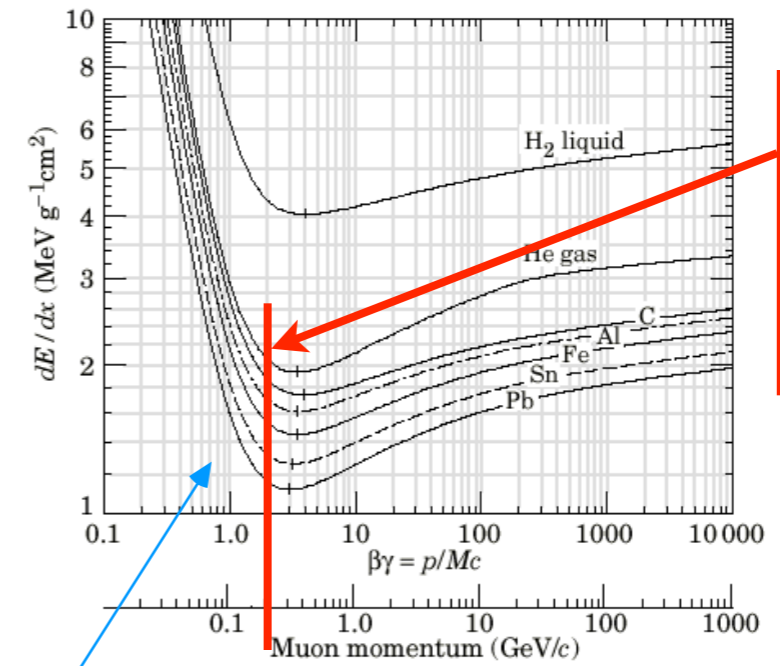
$$\begin{cases} E \rightarrow E - \left\langle \frac{dE}{dx} \right\rangle \Delta s \\ \theta \rightarrow \theta + \theta_{space}^{rms} \end{cases}$$

ionization energy loss  
multiple Coulomb scattering

- RF cavities between absorbers replace  $\Delta E$
- Net effect: reduction in  $p_{\perp}$  at constant  $p_{\parallel}$ , i.e., transverse cooling

$$\frac{d\epsilon_N}{ds} = -\frac{1}{\beta^2} \left\langle \frac{dE_{\mu}}{ds} \right\rangle \frac{\epsilon_N}{E_{\mu}} + \frac{\beta_{\perp} (0.014 \text{ GeV})^2}{2\beta^3 E_{\mu} m_{\mu} X_0}$$

(emittance change per unit length)



• ionization minimum is  $\approx$  optimal working point

• 2 competing effects  $\Rightarrow$  equilibrium emittance:  
 $\epsilon_0 \propto \beta_{\perp} / \langle dE/ds \rangle X_0$

- Only practical way to cool within  $2\mu s$   $\mu$  lifetime

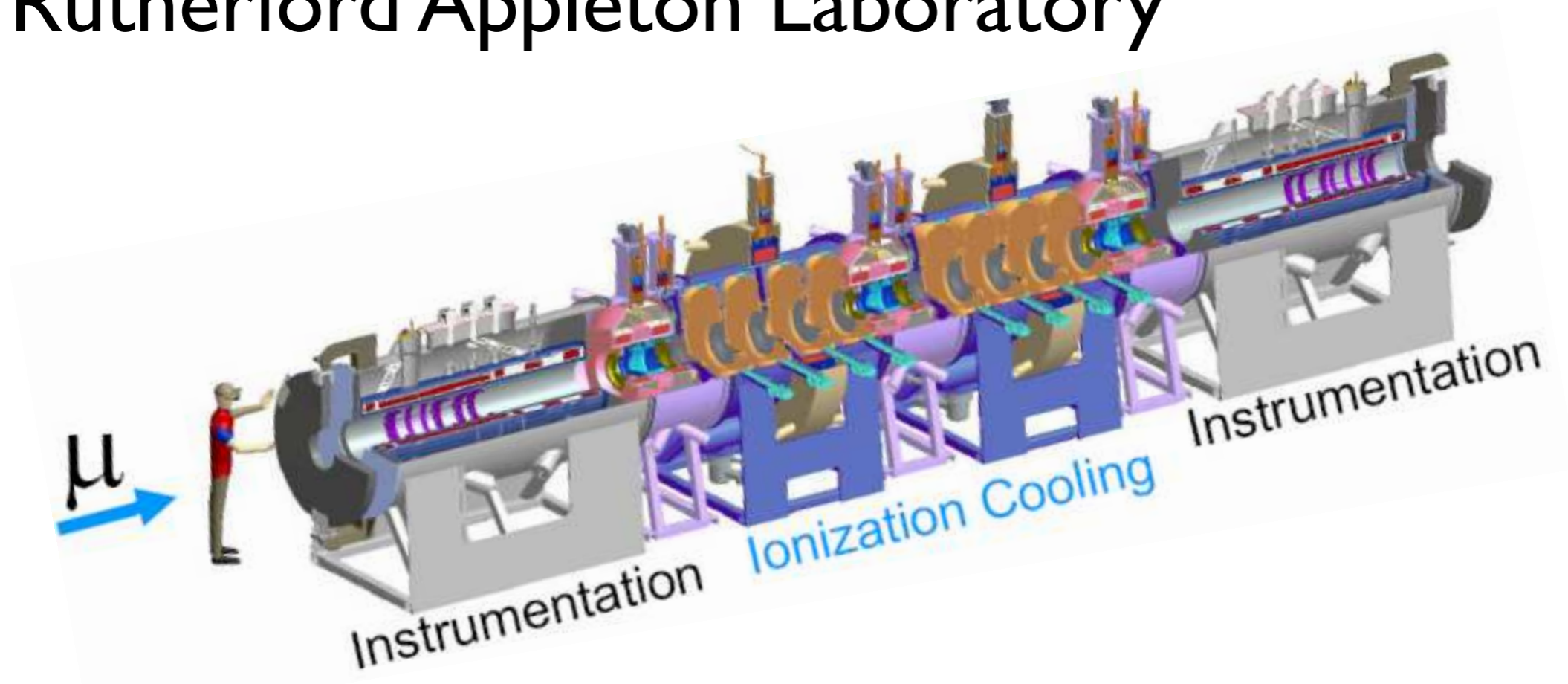
# Ionization Cooling

## Note:

- $dE/dx$  cooling mechanism inherently transverse
  - reduces  $p_x, p_y, p_z$  while acceleration replaces only  $p_z$   
⇒ cools only beam divergence
  - coupled to beam area by variable focusing  
→ 4D transverse cooling
- Demonstration in progress (MICE), 2013 goal...

# MICE

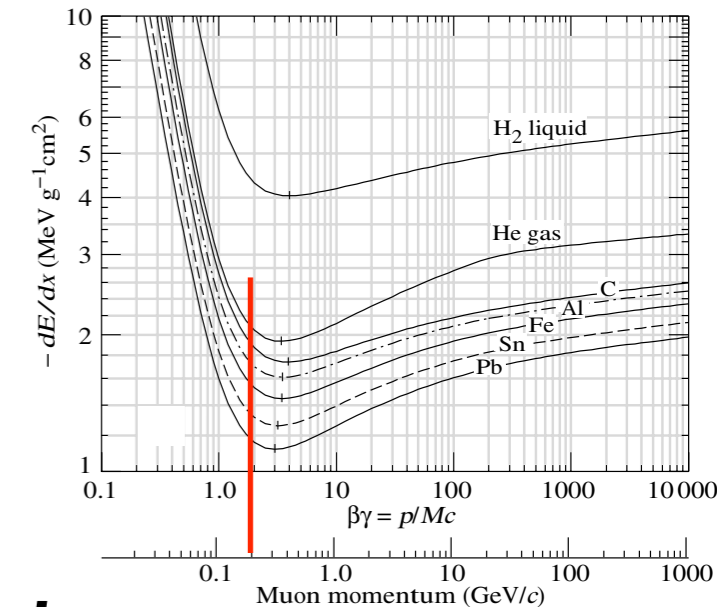
- Muon Ionization Cooling Experiment at UK's Rutherford Appleton Laboratory



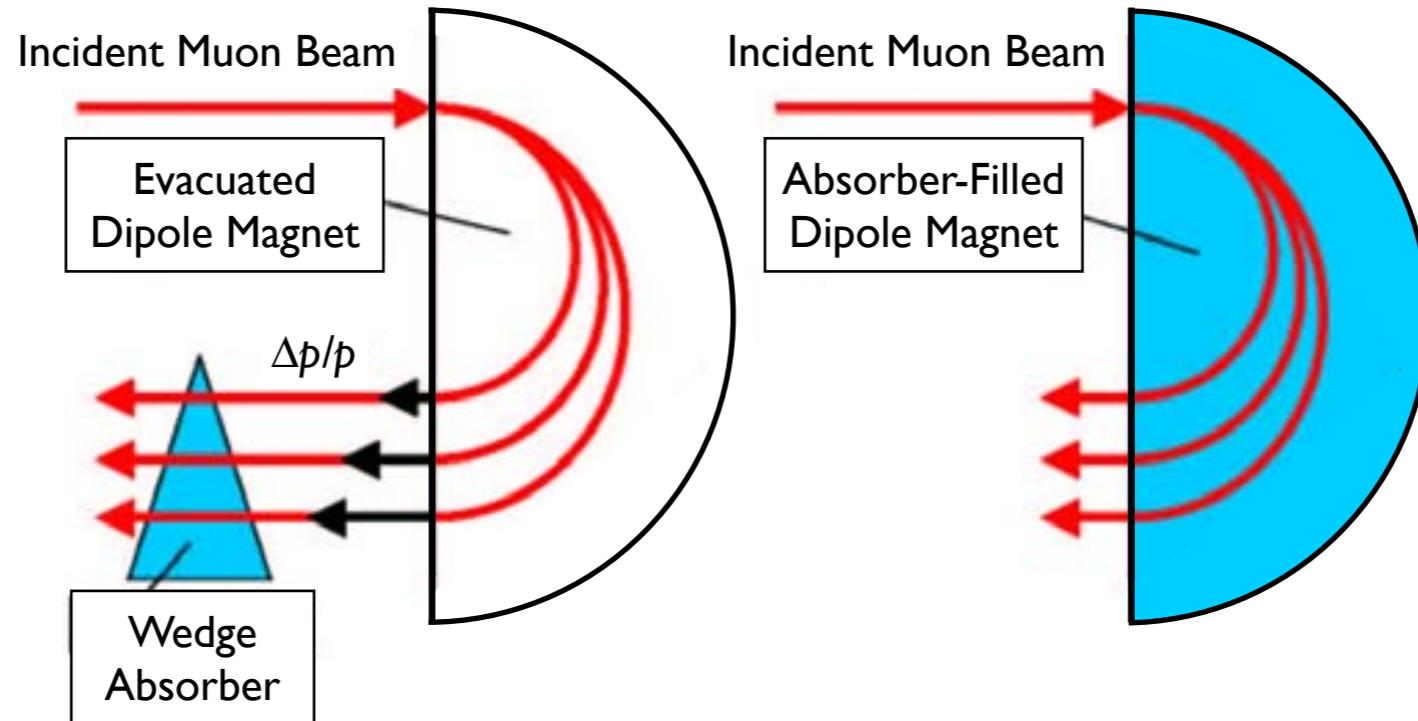
- Beamline working, apparatus buildup in progress
  - see WG3 parallel talks by Torun, Apollonio, Rayner

# How to cool in 6D?

- Work above ionization minimum to get negative feedback in  $p_z$ ?
- No – ineffective due to straggling



⇒ cool longitudinally via *emittance exchange*:



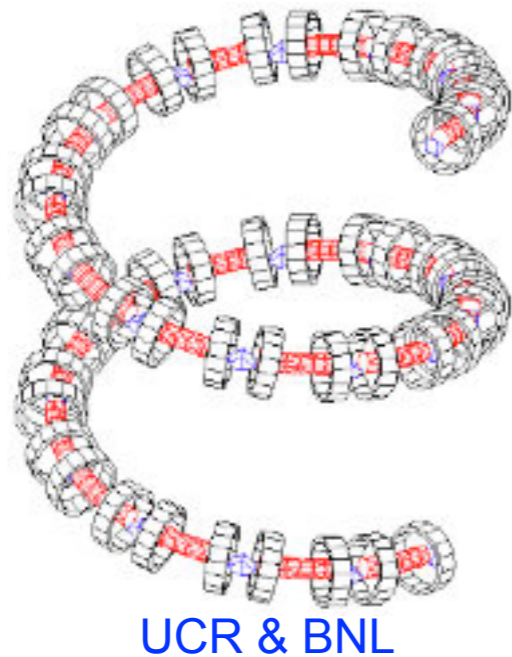
- Cool  $\epsilon_{\perp}$ , exchange  $\epsilon_{\perp}$  &  $\epsilon_{\parallel}$  → 6D cooling



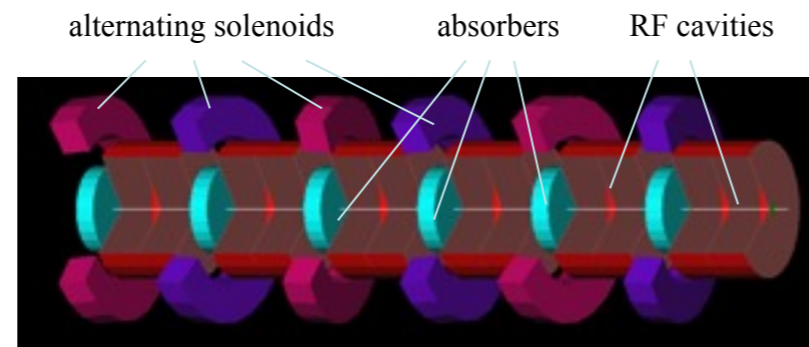
# How to cool in 6D?

- Tricky beam dynamics: must handle dispersion, angular momentum, nonlinearity, chromaticity, & non-isochronous beam transport
- After  $>10$  years of work, 3 solutions seem viable:

RFOFO "Guggenheim"

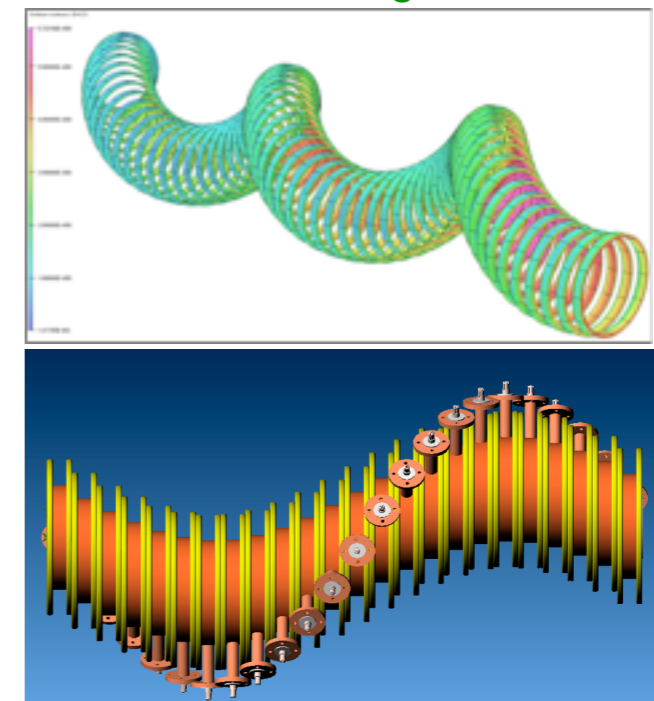


FOFO Snake



Y. Alexahin, FNAL

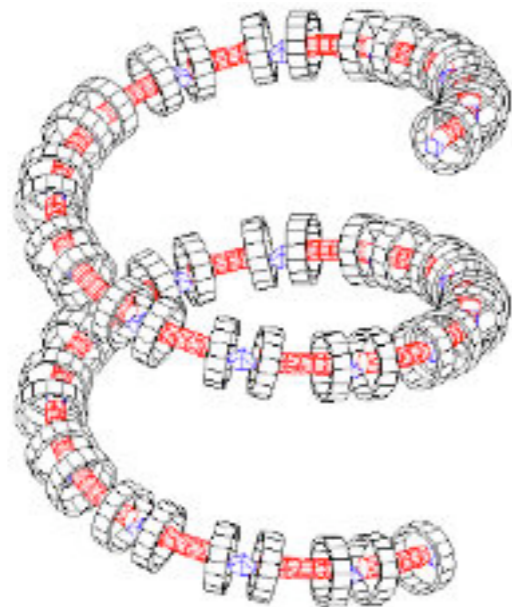
Helical Cooling Channel



# How to cool in 6D?

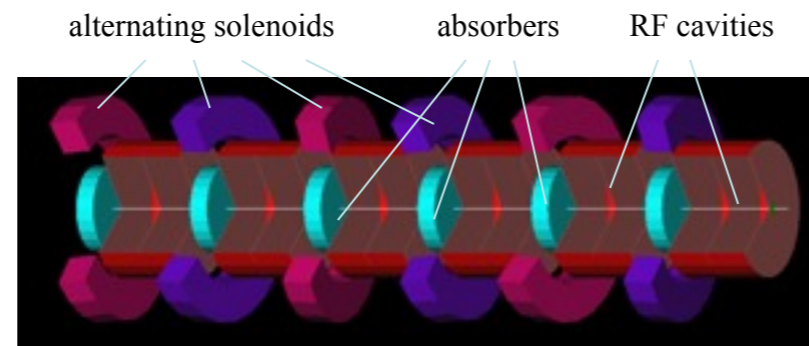
- After >10 years of work, 3 solutions seem viable:

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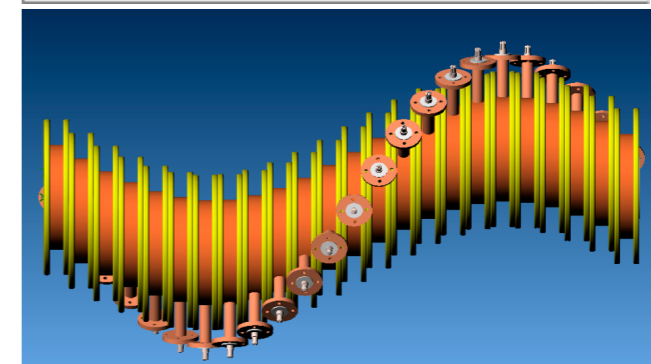
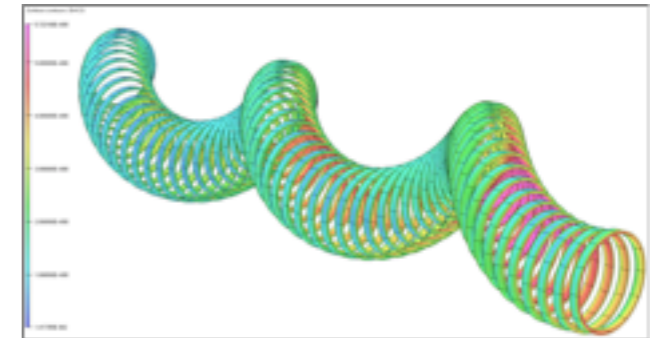
UCR & BNL

FOFO Snake



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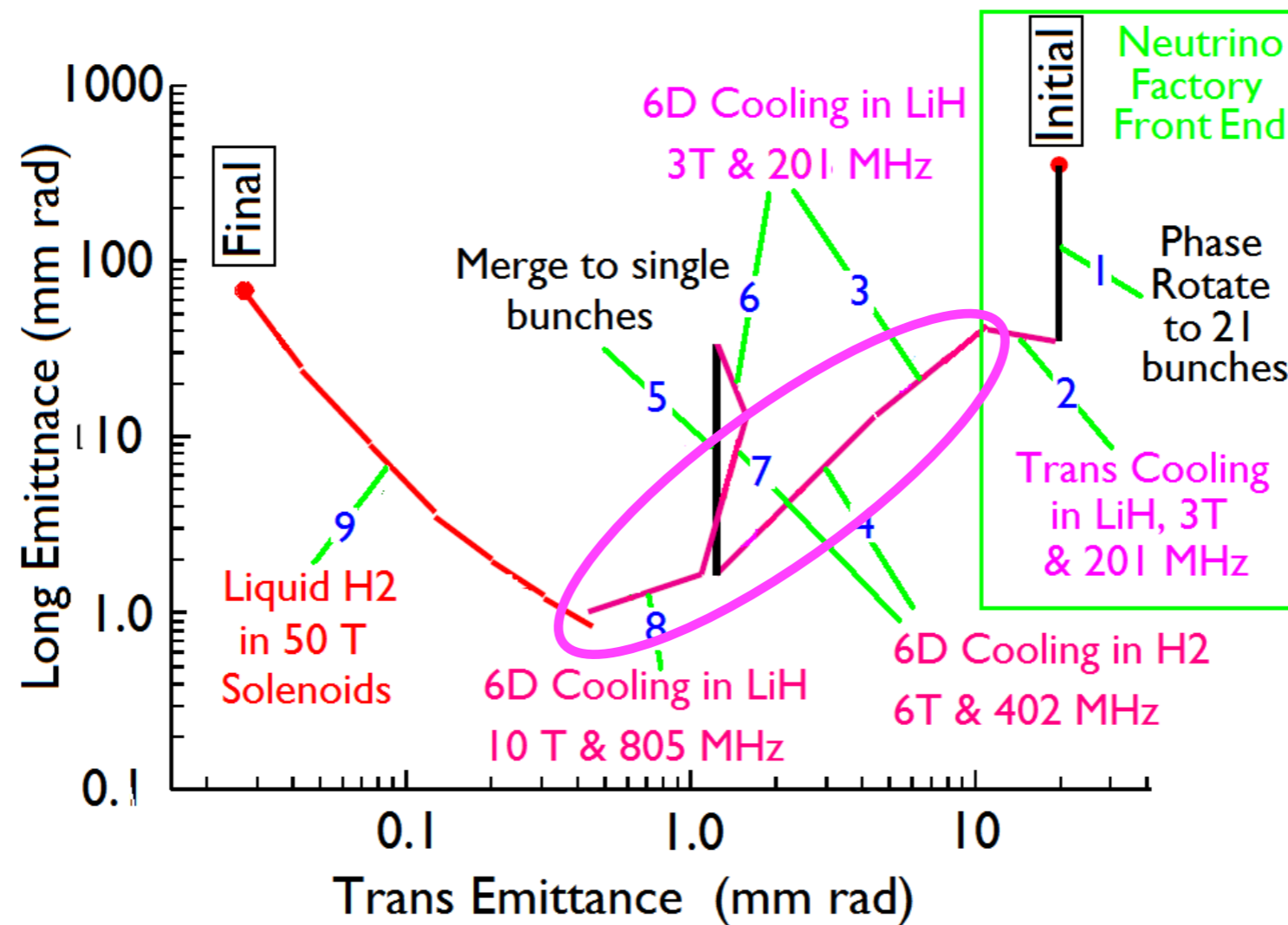


Muons, Inc. & FNAL

- FOFO Snake can cool both signs at once but may be limited in  $\beta_{\perp, min} \Rightarrow$  may be best for initial 6D cooling
- HCC may be most compact
- Not yet clear if all will work in practice, nor which is most cost-effective

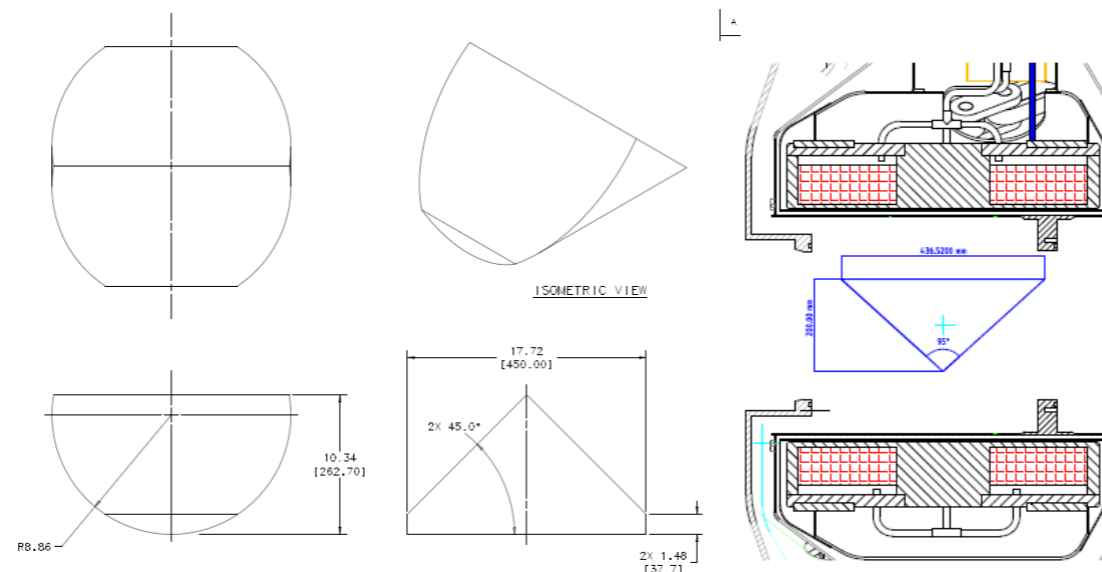
# How to cool in 6D?

- Guggenheim simulation results shown here



# 1st 6D cooling test:

- Some aspects of 6D cooling can be tested by inserting wedges in MICE
- Part of MICE program
  - have ordered LiH wedge:

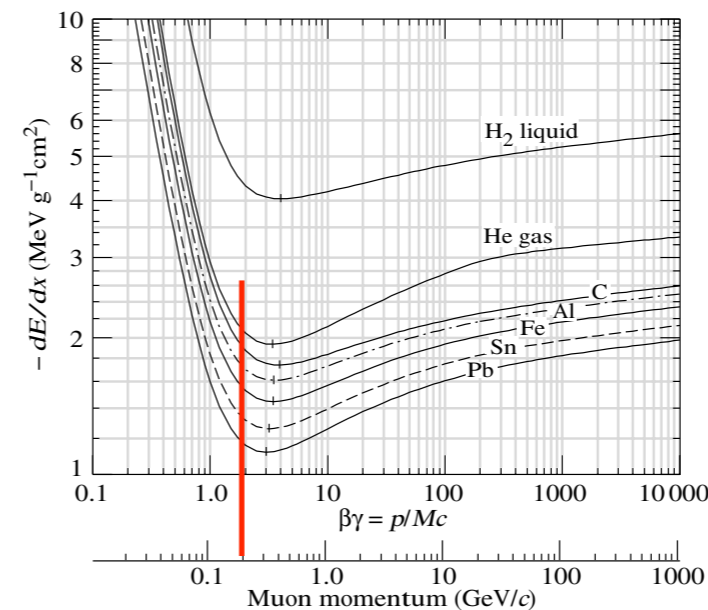


# Beyond 6D Cooling

- To reach  $\leq 25 \mu\text{m}$  emittance, must go beyond 6D cooling schemes shown above
- One approach (Palmer “Final Cooling”):
  - cool transversely in  $\sim 40 \text{ T}$   $B$  field at low momentum

- gives lower  $\beta$  & higher  $dE/dx$ :

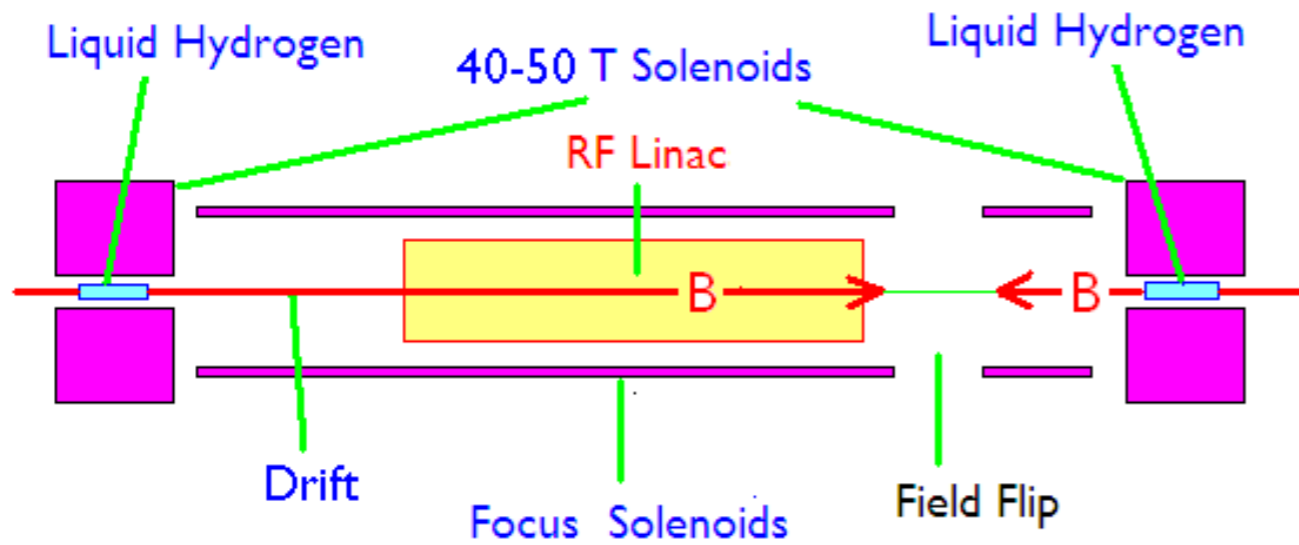
$$\beta_{\perp} \sim \frac{p}{B}$$



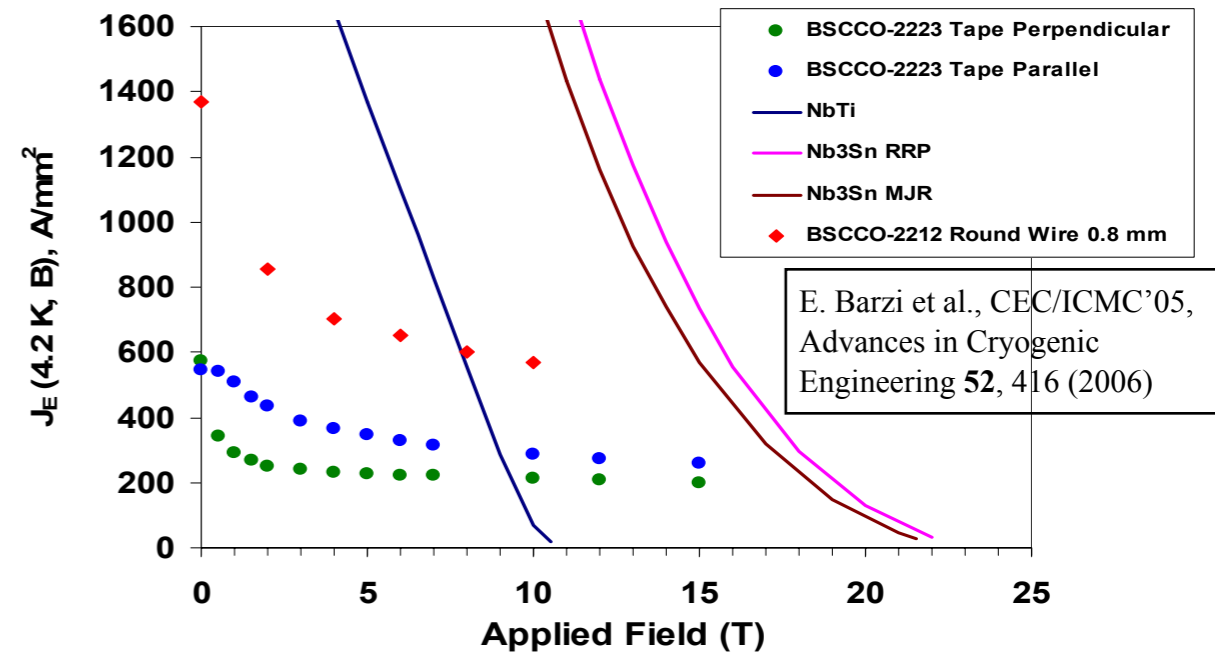
- Lower- $B$  options under study as well (Derbenev “PIC/REmEx,” lithium lenses)

# Final Cooling

- Palmer final-cooling cell:

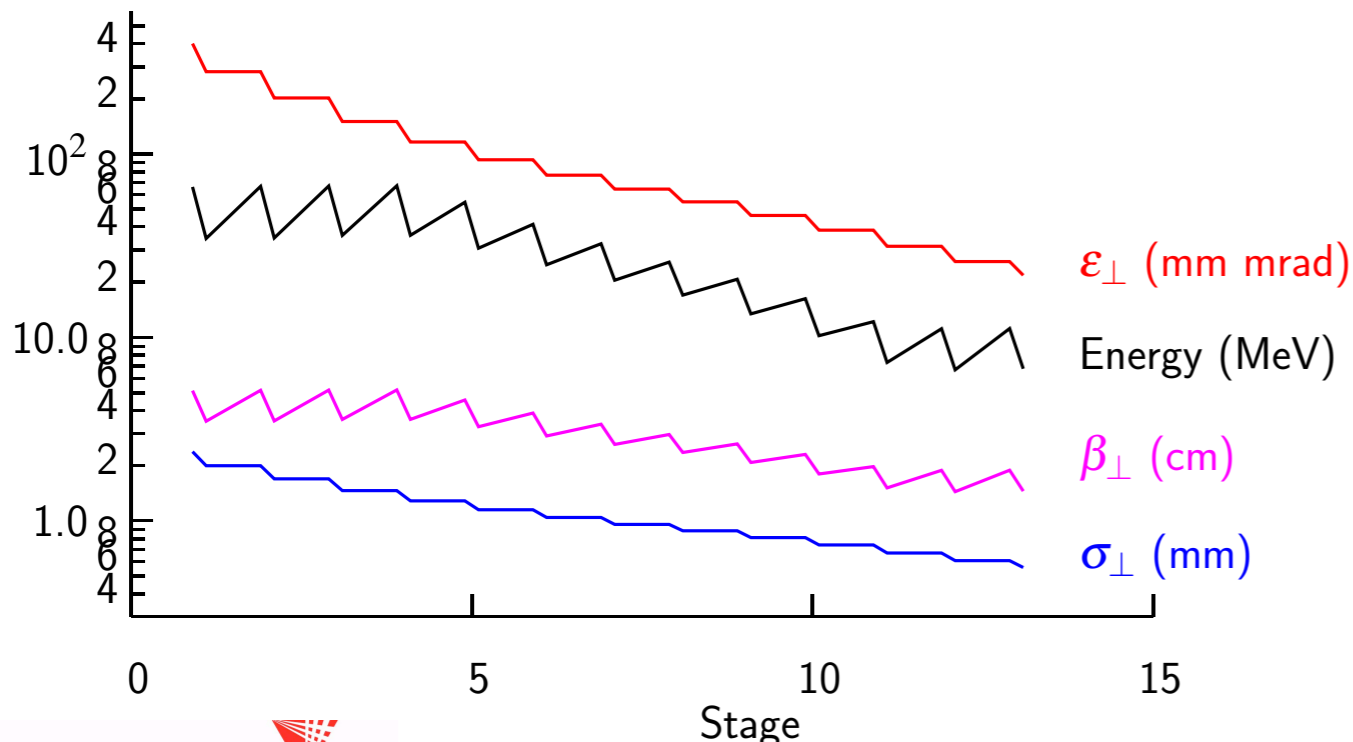


- HTS  $J_E$  @ 4.2 K quite flat vs B:



( $\exists$  YBCO 33.8 T hybrid solenoid @ NHMFL)

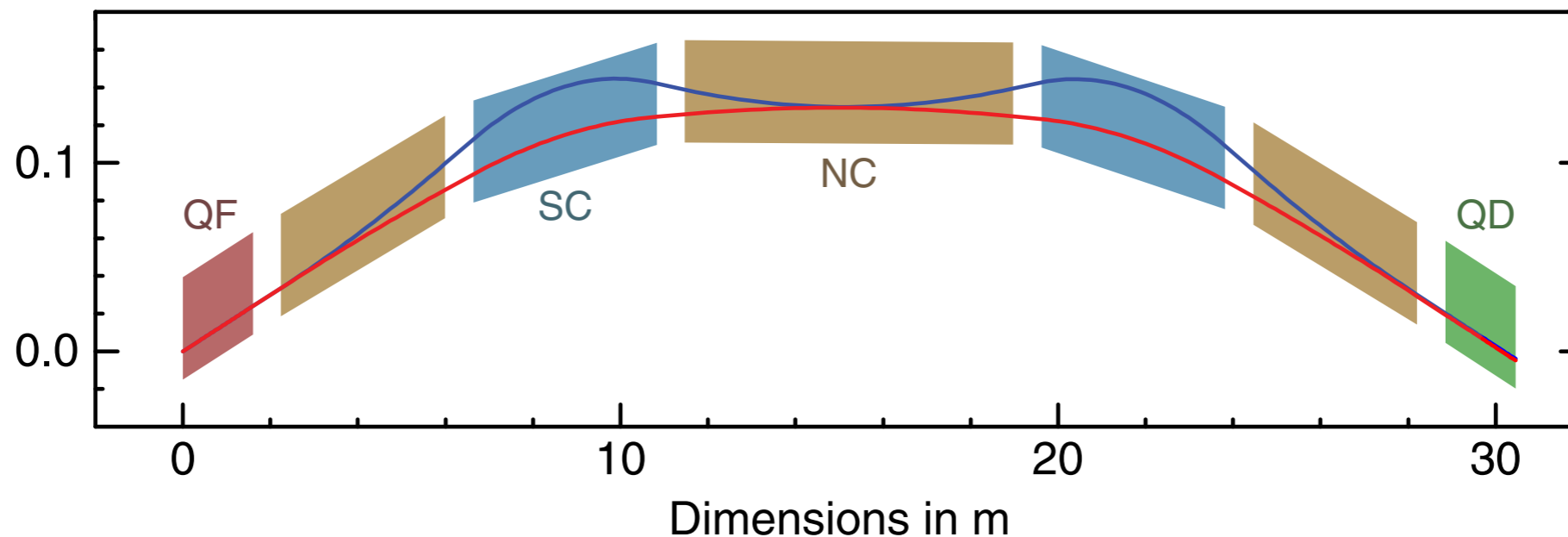
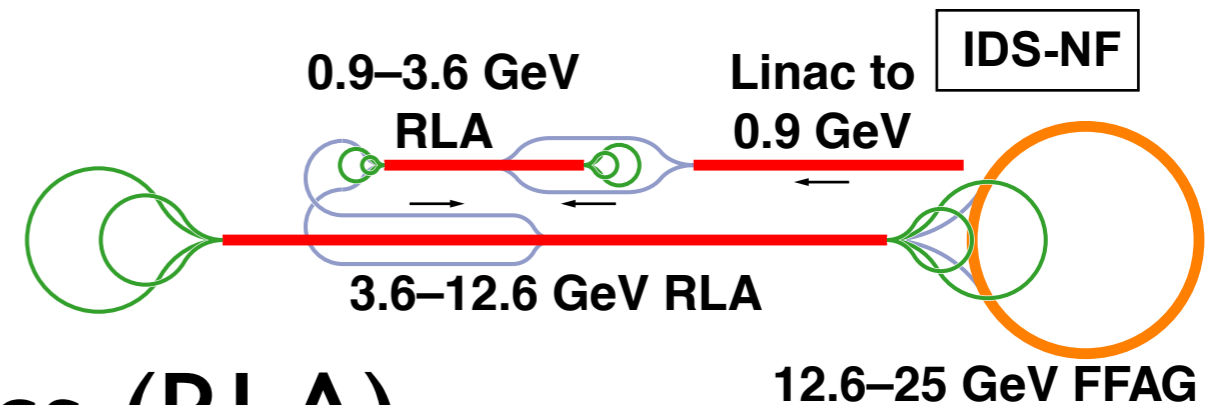
- Simulation of 13 stages:



- Beam energy falls from 70 MeV (135 MeV/c) to  $\approx$  6 MeV
- Bunch length rises from 5 cm to 300 cm rms
- Beam rms radius falls from 2 cm to 6 mm,  $\epsilon_{\perp}$  to 23  $\mu$ m
- 65% transmission

# Acceleration

- Initial linac
- Then recirculating linacs (RLA)
- Finally, rapid-cycling synchrotrons (RCS)
- Last RCS uses hybrid 8T SC and  $-1.8$  to  $+1.8$  T pulsed dipoles



# Collider Ring

- Example 2.5 km storage ring for  $\sqrt{s} = 1.5$  TeV:

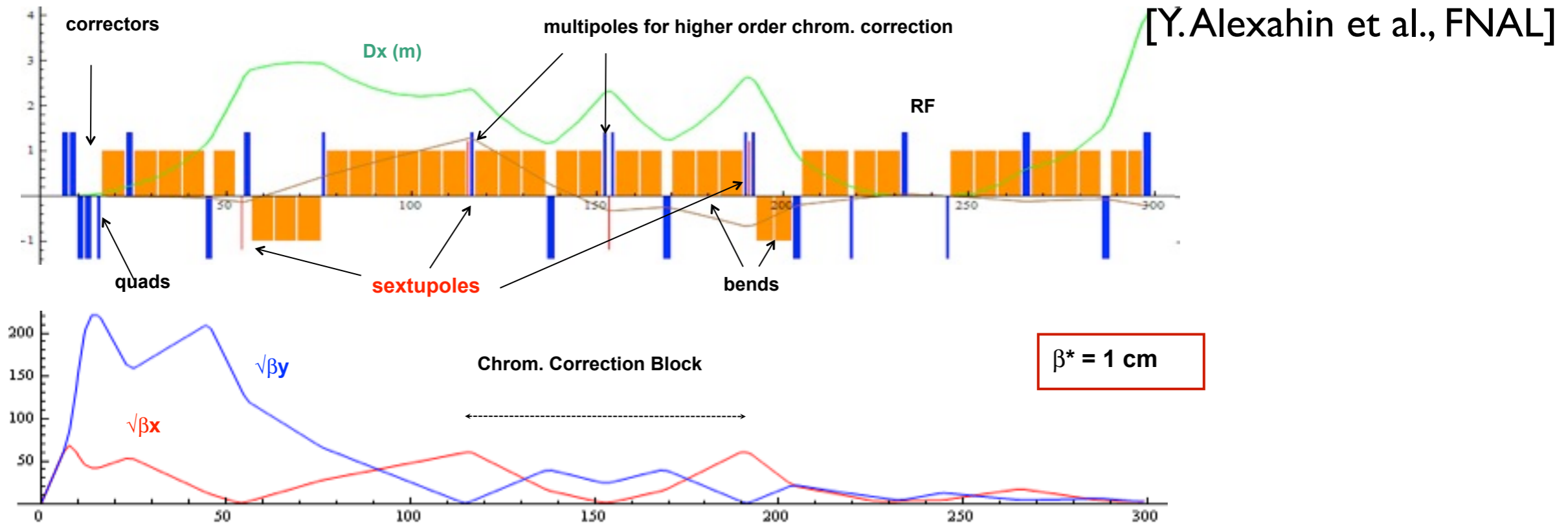


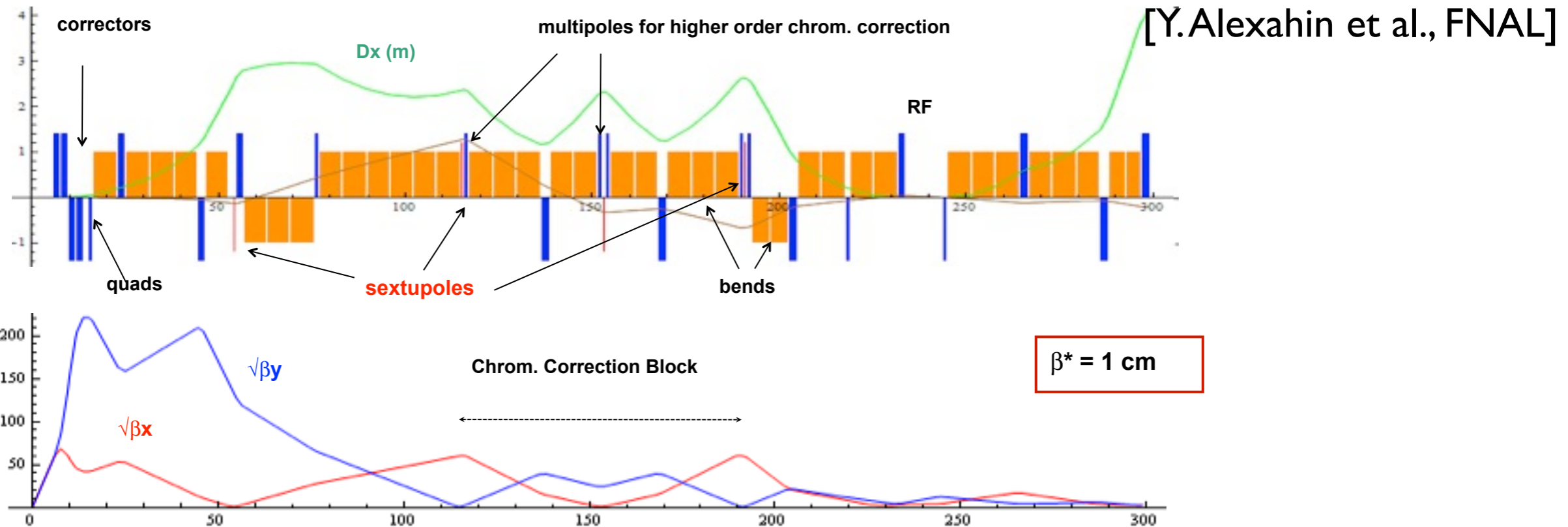
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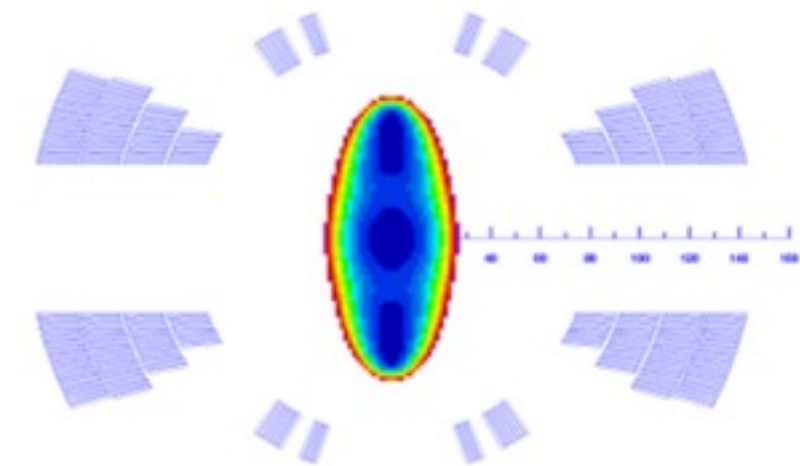


# Collider Ring

- Example 2.5 km storage ring for  $\sqrt{s} = 1.5 \text{ TeV}$ :



- Employs open-midplane dipoles (8 & 10 T) in order to cope with decay electrons
- Will continue to be refined



# Conclusions

- A high- $\mathcal{L}$  Muon Collider is probably feasible, and buildable as a Neutrino Factory upgrade
  - whether things go in this order remains to be seen!
- Requires development of high-field HTS solenoids
- Technology selection, feasibility demonstration, and cost estimation are main goals of MAP 7-year program

# Acknowledgments

- My thanks and congratulations to Naba and the organizing committee for an exciting, memorable, and smoothly run workshop!