

Low emittance, slow muon source for new g-2 experiment

K. Ishida (RIKEN) for
New g-2/EDM@J-PARC collaboration

What is this for?

Requirement on ultra cold muon beam for new g-2

Development plans

- Search of thermal muonium emission target

- (S1249 Experiment @ TRIUMF)

- Laser and acceleration developments

Motivation of this development

Realizing muon storage ring without focusing electric or magnetic field for muon g-2

1. new muon g-2 measurement

complimentary and with higher precision to BNL E821

2. Requirement : ultra cold muon beam

$\sim 300 \text{ MeV}$, $\Delta p_T/p_L \sim 10^{-5}$

Why muon g-2?

magnetic moment

$$\vec{\mu} = g \left(\frac{e}{2m} \right) \vec{s}$$

m : magnetic moment

s : spin

g : gyromagnetic ratio

Dirac equation : g=2

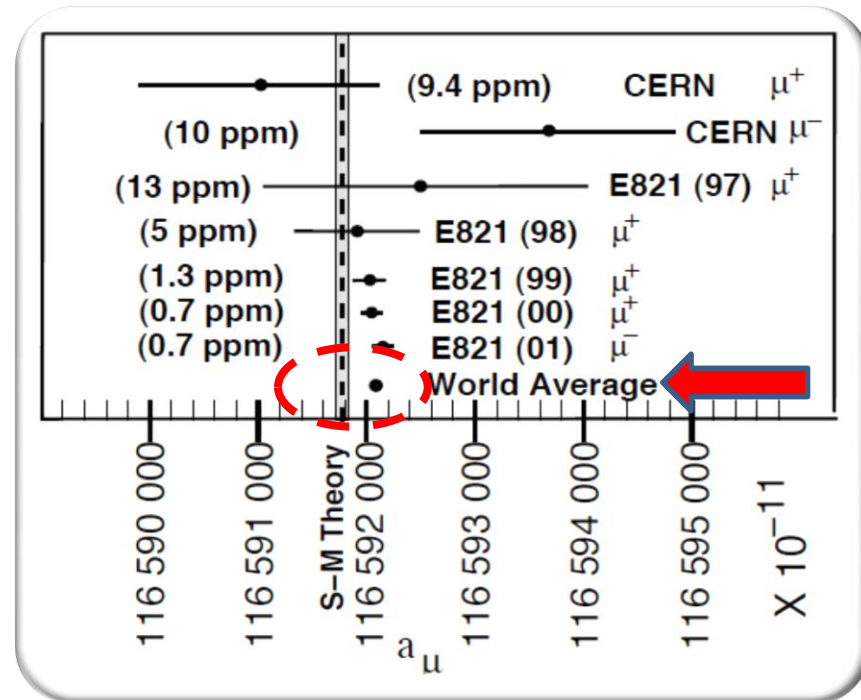
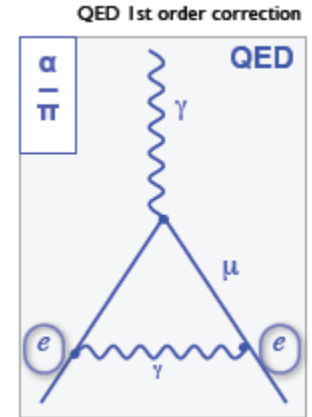
$$\mu = (1 + a) \left(\frac{e\hbar}{2m} \right)$$

QED correction

$$a = \frac{g-2}{2} = \frac{1}{2} \left(\frac{\alpha}{\pi} \right) - 0.3248 \left(\frac{\alpha}{\pi} \right)^2 + \dots$$

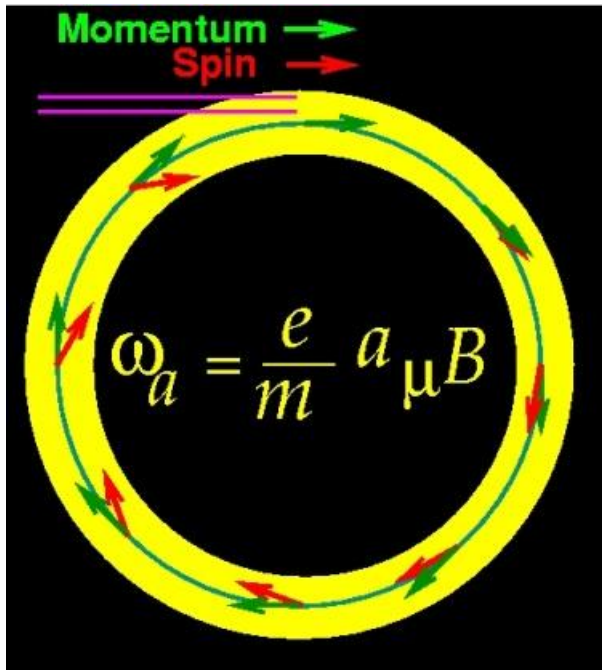
Inconsistency observed at BNL E821

$$\Delta a_{\mu}^{(\text{today})} = \Delta a_{\mu}^{(\text{Exp})} - \Delta a_{\mu}^{(\text{SM})} = (295 \pm 88) \times 10^{-11}$$



How to measure $a_\mu = (g-2)/2$

Detect the muon precession frequency in the uniform magnetic field \vec{B}



$$\vec{\omega}_a = \vec{\omega}_s - \vec{\omega}_c = \frac{e}{m_\mu} \left(\frac{g_\mu - 2}{2} \right) \vec{B} \quad \vec{\omega}_a = \frac{e}{m_\mu} a_\mu \vec{B}$$

$$\frac{\Delta a_\mu}{a_\mu} = \frac{\Delta \omega_a}{\omega_a} \oplus \frac{\Delta B}{B}$$

< 0.1 ppm

< 0.1 ppm

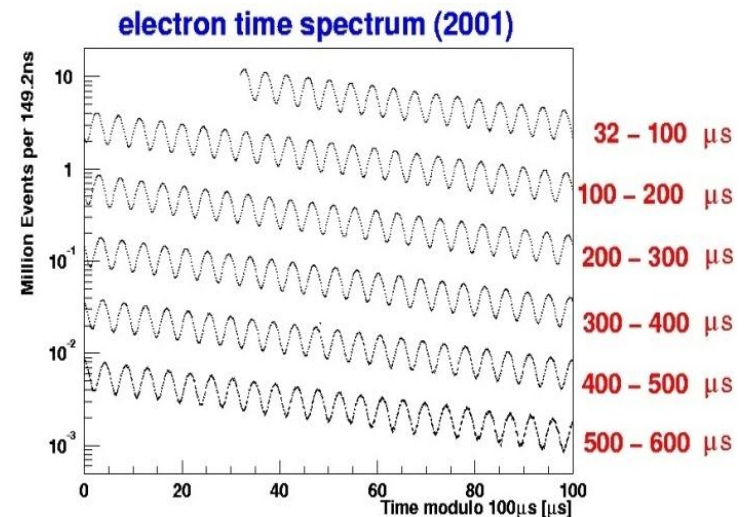
BNL muon g-2 experiment

Muon storage ring with homogeneous magnetic field
+ Muon focusing by electric quadrupoles
using **magic momentum (3.09 GeV/c)**

$$\vec{\omega}_a = -\frac{e}{m_\mu} \left[a_\mu \vec{B} - \left(a_\mu - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right]$$

Typical storage ring diameter 14m

Statistically limited but systematic error will also contribute
high energy pion contamination, field homogeneity of large magnet, ...



New muon g-2 proposal using ultra-cold muon beam

N. Saito's talk in WG4, NuFact09

Muons with very small transverse momentum stay in storage ring orbit even **without focusing electric field**.

-> no need of magic momentum (3.1 GeV/c)

$$\vec{\omega}_a = -\frac{e}{m_\mu} \left[a_\mu \vec{B} - \left(a_\mu - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right]$$

-> but reasonably high γ (300 MeV/c)

will help statistics (longer dilated lifetime)

Benefits: Compact muon ring – better B field

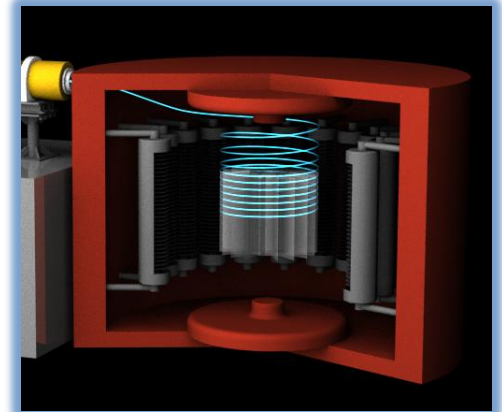
Compact detectors – better resolution

Clean muon beam - no pion flash

Essential requirement is

high-intensity ultra-cold (well-aligned) muon beam

g-2@J-PARC (~0.8m)



Requirement on ultra-cold muon beam for g-2

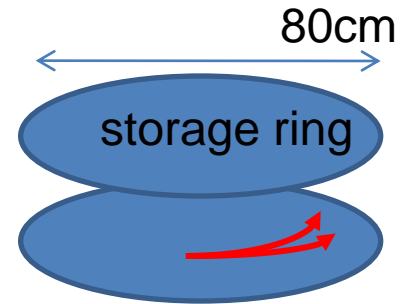
Small beam divergence

$$\sigma(p_T)/p_L = 10^{-5}$$

will limit vertical spread in muon g-2 storage ring to 80 mm after 4000 turns ($\sim 5 \gamma \tau_\mu$)

For $p_L=300$ MeV/c (storage in 3T compact ring ~ 80 cm),

p_T should be < 3 keV/c ($T \sim 0.045$ eV = 500K)



This could be achieved by stopping muons in a target and accelerating muons reemitted from its surface.

Slow muon from hot tungsten (2100 K) is not cold enough without additional beam cooling.

We would better start with **muonium emission at room temperature.**

3 GeV proton beam
(333 μA)

Graphite target
(20 mm)

Surface muon beam
(28 MeV/c, $4 \times 10^8/\text{s}$)

Muonium Production
(300 K \sim 25 meV)

Muon LINAC
(300 MeV/c)

New Muon g-2/EDM Experiment at
J-PARC with Ultra-Cold Muon Beam

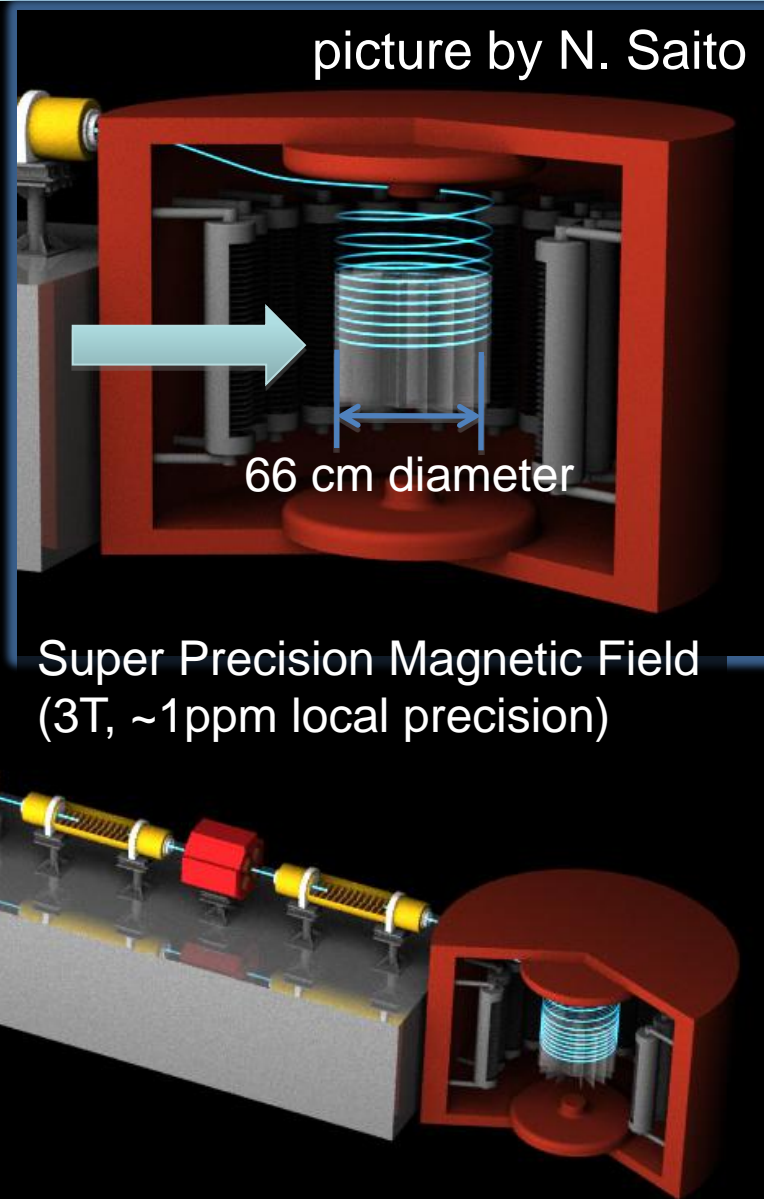
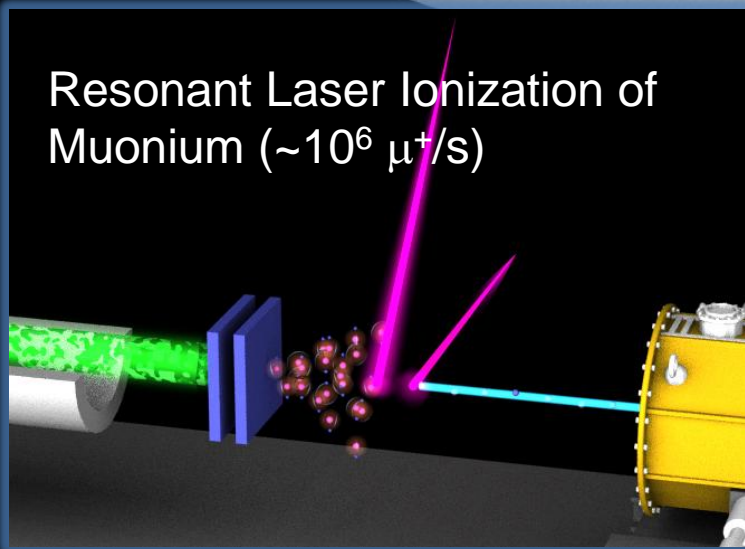
picture by N. Saito

Silicon Tracker

66 cm diameter

Super Precision Magnetic Field
(3T, \sim 1ppm local precision)

Resonant Laser Ionization of
Muonium ($\sim 10^6 \mu^+/\text{s}$)



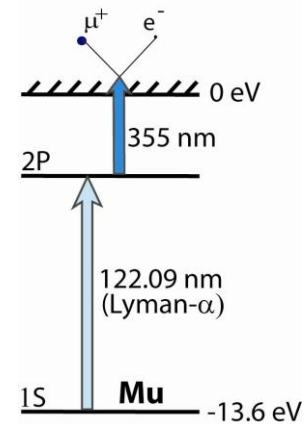
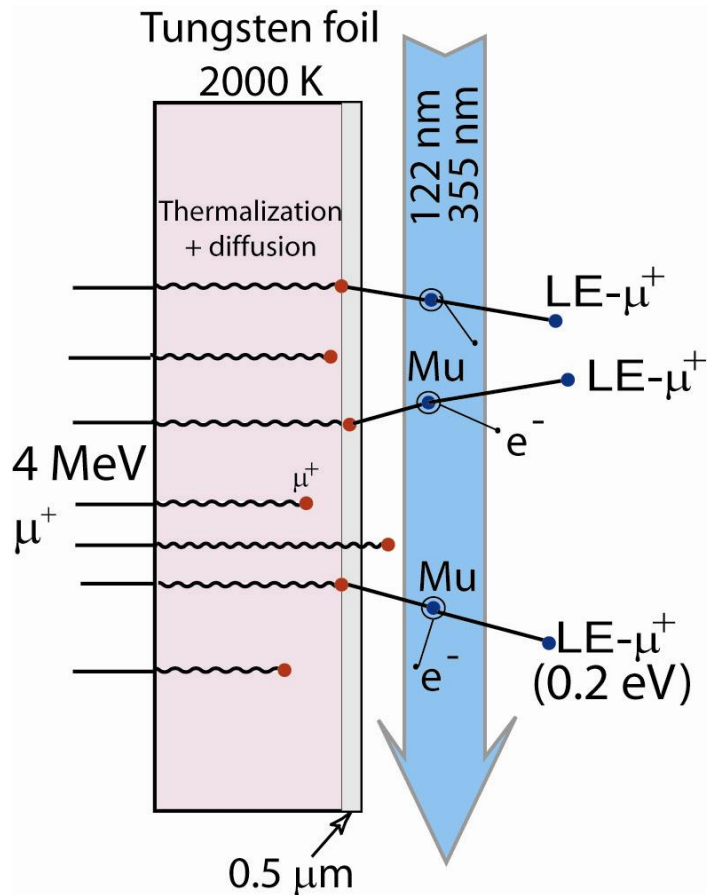
Comparison of g-2 measurements

	BNL-E821	Fermilab	J-PARC
Muon momentum	3.09 GeV/c		0.3 GeV/c
gamma	29.3		3
Storage field	B=1.45 T		3.0 T
Focusing field	Electric quad		None
# of detected μ^+ decays	5.0E9	1.8E11	1.5E12
# of detected μ^- decays	3.6E9	-	-
Precision (stat)	0.46 ppm	0.1 ppm	0.11 ppm

g-2@J-PARC based on 10^6 /s cold muons, 1 year run
How to achieve this?

Development of thermal muon source at KEK/RIKEN-RAL

4 MeV muons $\xrightarrow{2\%}$ 0.2 eV thermal Mu $\xrightarrow{\quad}$ 0.2 eV μ^+



122.09 nm (Mu)
121.57 nm (H)
121.53 nm (D)

- **two** laser beams necessary for resonant ionization
- required very broad laser bandwidth due to thermal movement of atoms

1S-2P saturation intensity

$I_{\text{sat}} = 2.3 \text{ W/cm}^2$ $\xrightarrow{\quad}$ $I_{\text{sat}} = 4.6 \text{ kW/cm}^2$
monochromatic < 100 MHz (Doppler 200 GHz)

Main challenge: to generate VUV @ 122 nm and with 200 GHz (+ 1 ns jitter rel. to ext. trig.)

Slow muon beam: present status

Achievement at RIKEN-RAL by KEK-RIKEN Collaboration

Low energy μ^+ beam

Slow muon beam intensity $\sim 15\text{-}20 \mu^+/\text{s}$
(starting from 1.5×10^6 muons)

Beam diameter (FWHM): 4 mm

Energy at target region 0.2 eV

Energy after re-acceleration 0.1-18 keV

Energy uncertainty

after re-acceleration ~ 14 eV

Pulse repetition rate 25 Hz

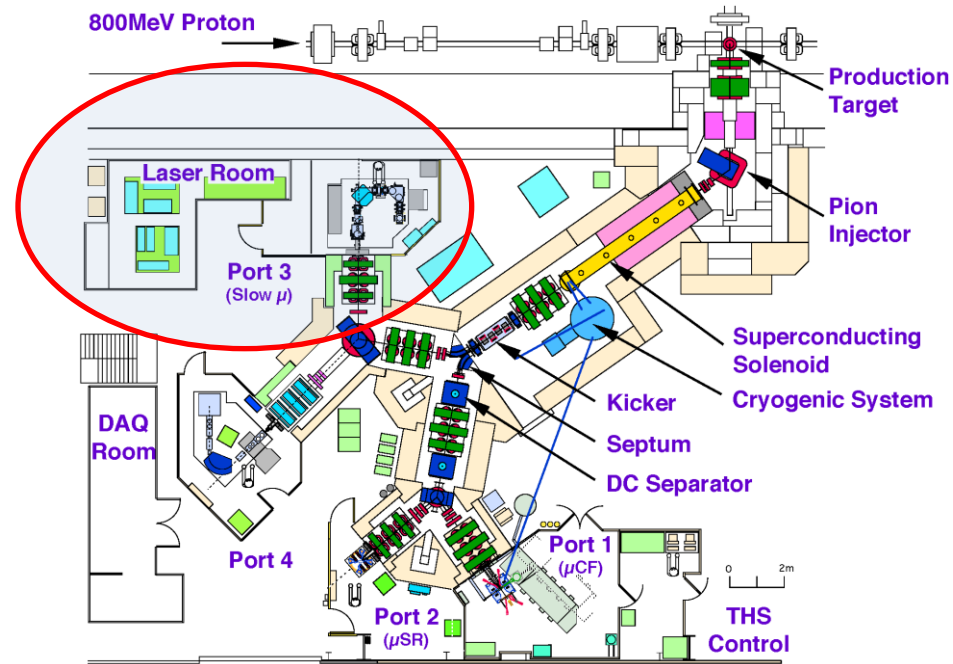
Single pulse structure

7.5 ns (FWHM) at 9.0 keV

Spin polarisation $\sim 50\%$

Long time background $< 1/250$

Rutherford Appleton Laboratory
200 kW proton source



Overall efficiency was 10^{-5} based on hot tungsten target (2100 K)

We need lots of improvement in intensity and properties

Prospect for increasing the ultra-cold muon intensity for the new muon g-2

We aim 20/s => 10^6 /s ultra cold muon beam for muon g-2.

1. Stopped muon intensity (density)

-> Super omega & J-PARC (x300) (Miyake, Ikedo@NuFact10)

=> $1 \sim 4 \times 10^8$

+ Tapered tube (x2 ?) (Tomono@Nufact10 tomorrow)

2. Muonium emission efficiency (x1?)

0.04 (@2100K) -> ? (room temperature materials)

test of candidate materials at TRIUMF

3. Laser ionization & repetition

S. Wada, Norihito Saito, K. Yokoyama, O. Louchev (x100 x2) => 0.2

4. Ultra-cold muon extraction optics (acceleration without heating)

design@RIKEN (M. Iwasaki, K. Tsukada) (~1 ?)

=> 10^6 /s

Mu producing materials

Two types of materials have been used so far

Hot tungsten (@2100 K)

Fast diffusion in thin W to surface at high temperature

Efficiency $\sim 4\%$ (4 MeV μ beam to Mu)

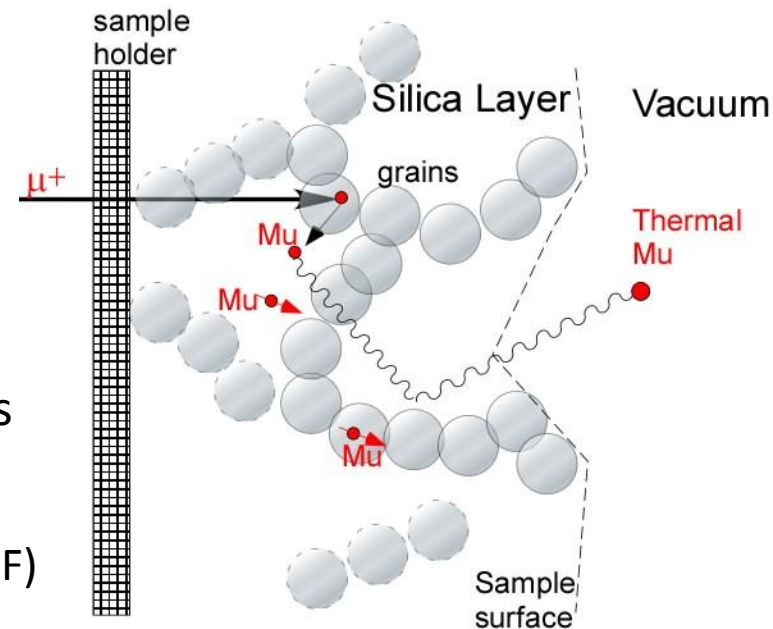
utilized for slow muon beam (KEK, RIKEN-RAL)

Silica Powder (@300 K)

Rapid diffusion in spaces between nano-particles

Efficiency $\sim 4\%$

utilized for Mu 1S-2S(KEK, RAL), Mu-Mubar(PSI, LAMPF)



Comparison of Mu production from Hot W and Silica powder

	Hot W	Silica Powder
	2100K	300K
Energy spread	0.2 eV	x 1/7
Transverse momentum	6 keV/c	x 1/2.6
Doppler width	20 GHz	x 1/2.6
Mu area	large	small
Mu separation	large	small
Yield	3%	3%
Purity	High & stable	?
Heat emission	Large	none
Shape stability	could bend	need settle

-> Many advantages with room temperature target:
smaller source size, less Doppler broadening, ...

Plan for Muonium Production Target Study

Silica powder is known to produce muonium at room temperature but it's **very fluffy** and **difficult to hold**

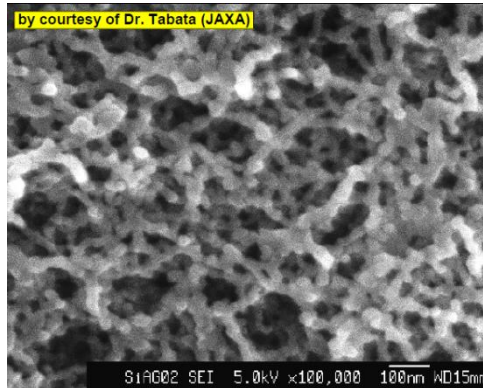
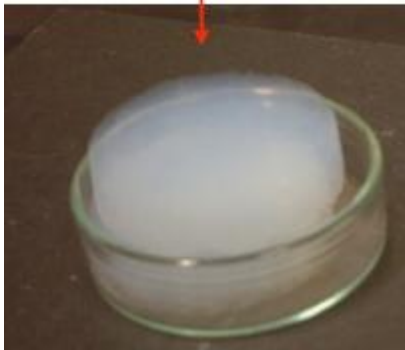
We made several **new solid targets** with porous structure to study



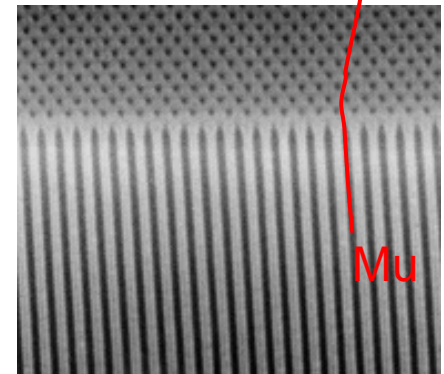
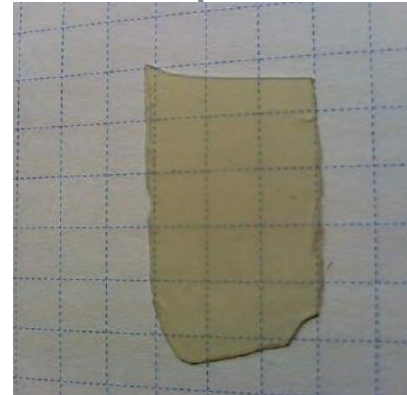
2

G.M. Marshall

silica aerogel



porous alumina, silica



Measurement of muonium emission yield by imaging

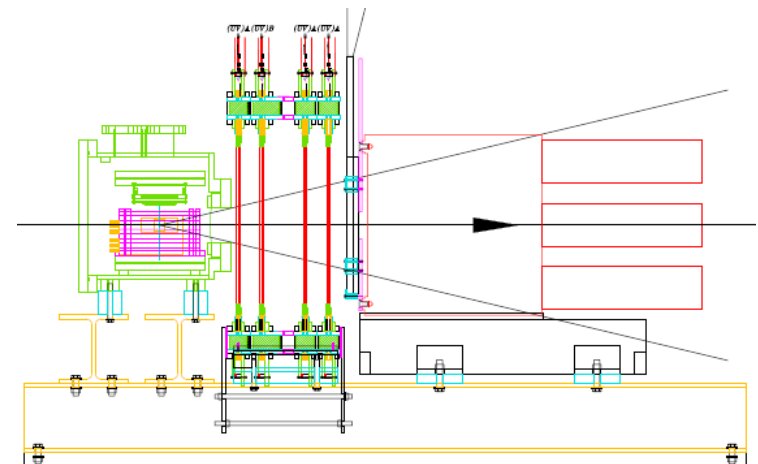
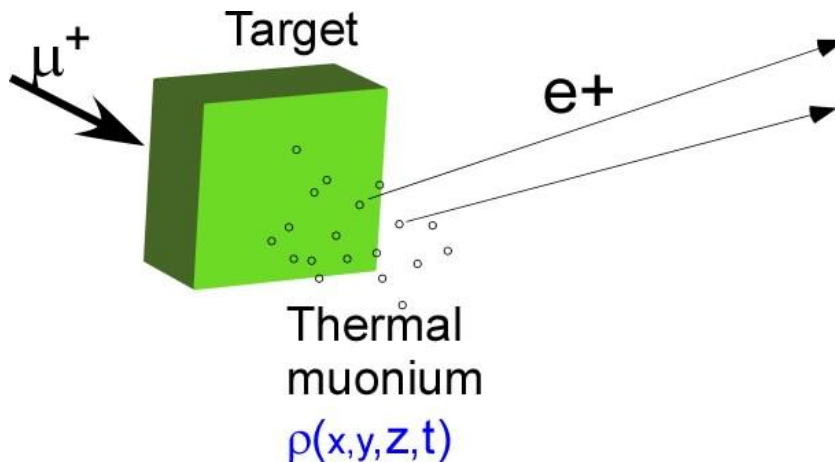
Muonium imaging to measure muonium yield and profile.

(Measurement at TRIUMF by RIKEN/KEK/TRIUMF collaboration in this November)

1) **Thermal muonium yield** for various target => which gives best yield?

2) **Spatial distribution of Mu vs timing (laser)**

=> When and where can we effectively shoot ionizing laser?



Previous measurement on SiO_2 powder

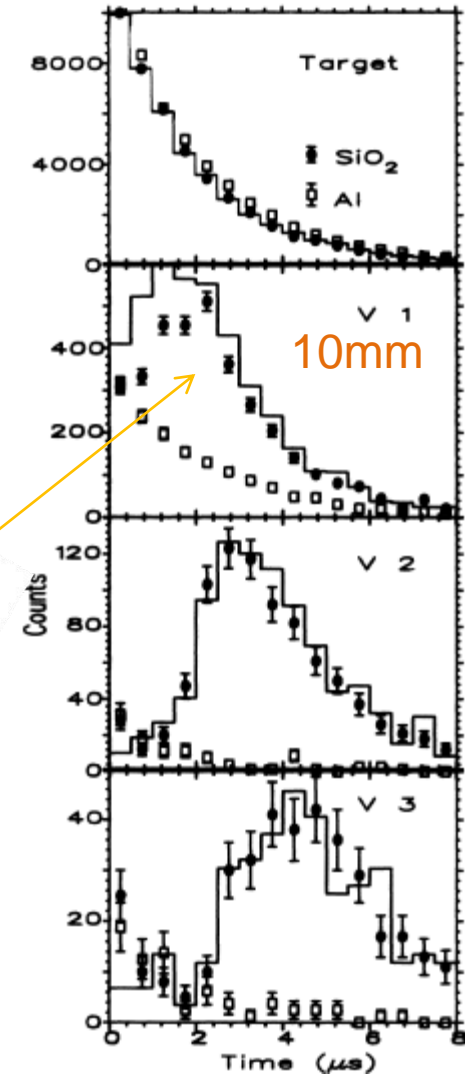
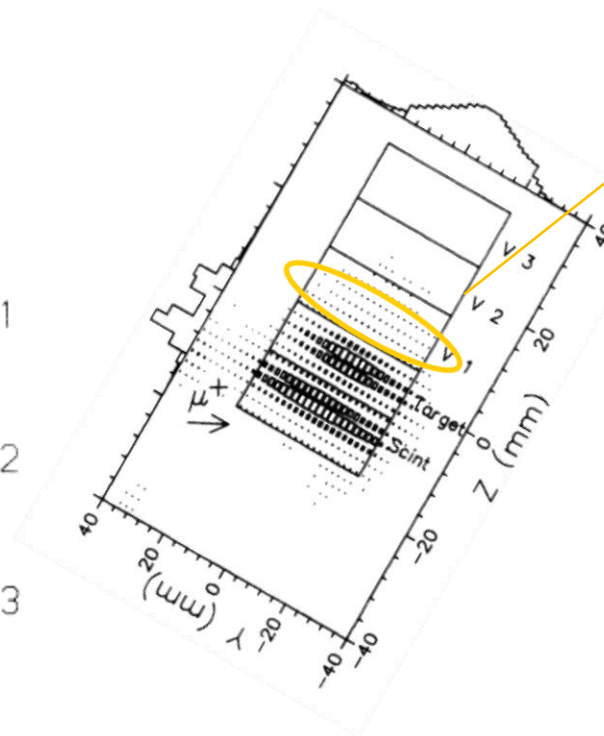
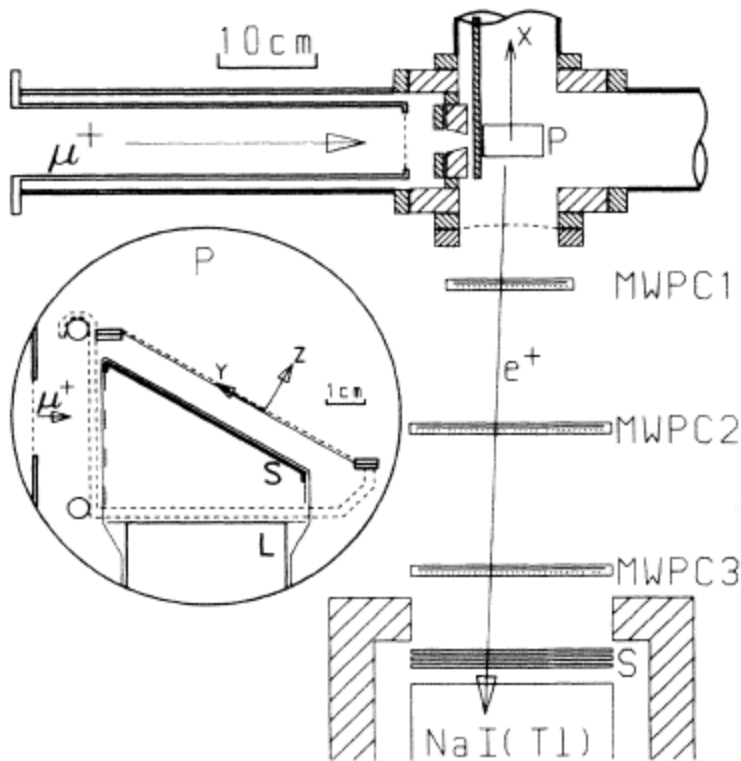
Typical measurement

Beer et al, Phys.Rev.Lett. 57 (1986) 671

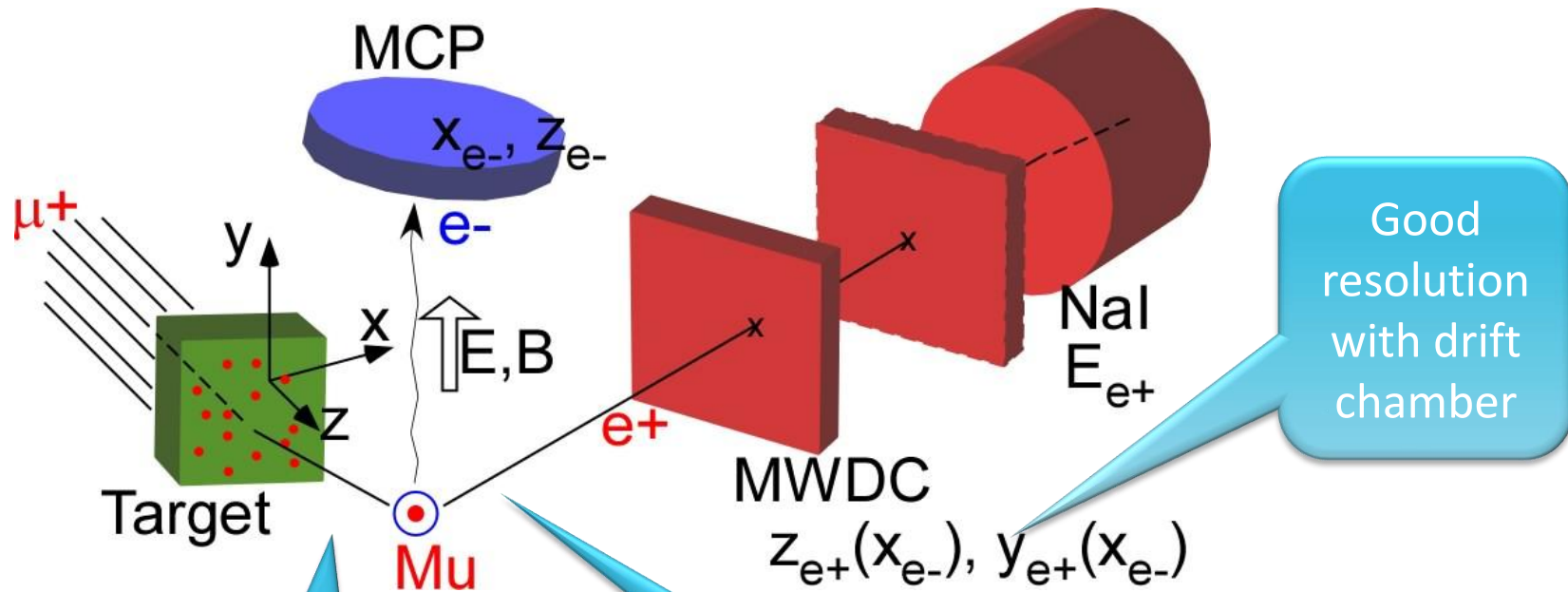
Vacuum chamber + Target + MWPC

– analysis based on 4 regions (each 10mm thick)

measurement close target surface suffered from background



Significant improvements expected with MWDC, MCP



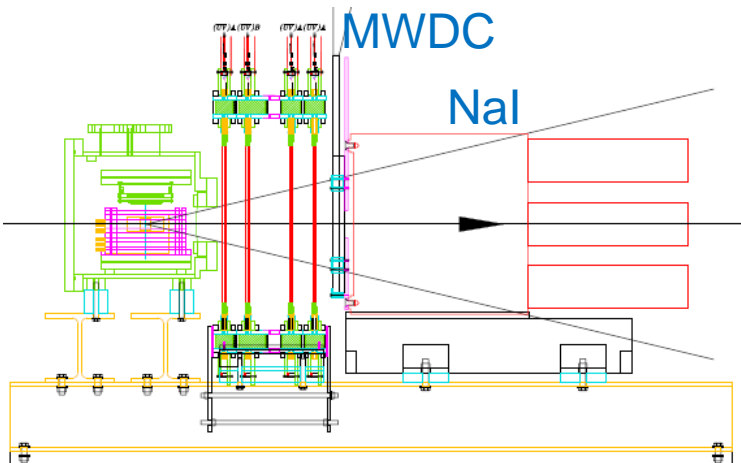
Detection of electron also rejects a huge BG from μ decay in target without e^-

Complete reconstruction of 3D coordinates of decay vertex from e^+ in coincidence with e^-

Good resolution with drift chamber

Status of Preparation (1)

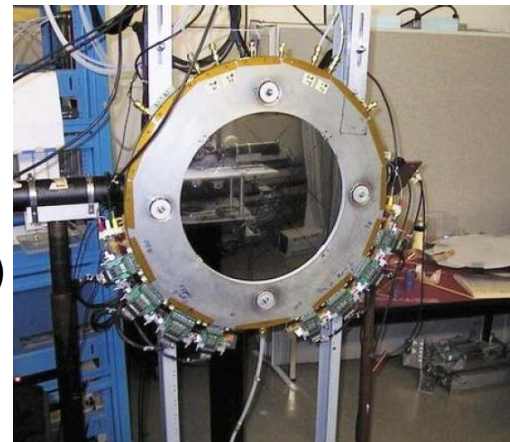
at TRIUMF



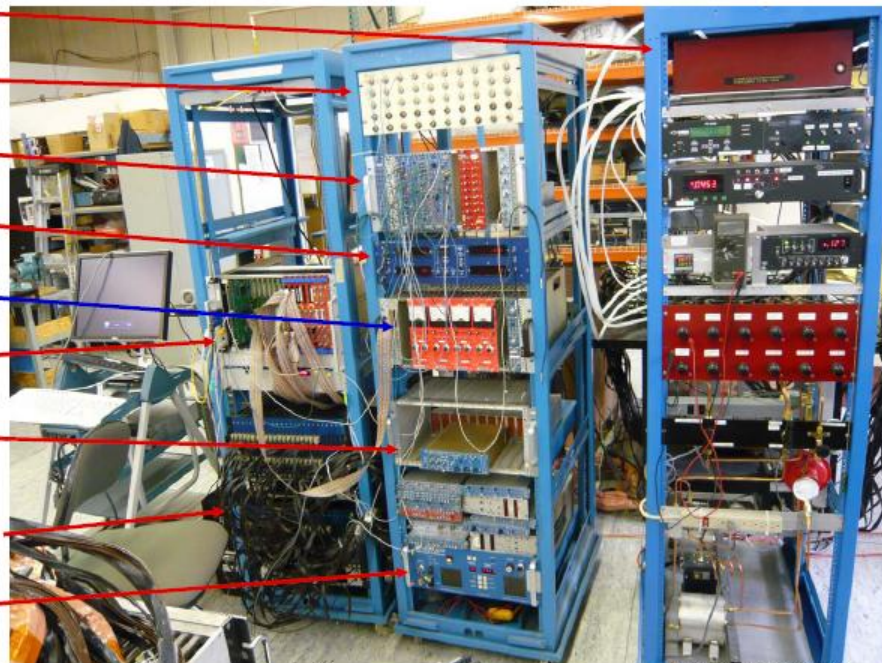
Mount table
(from Tokyo Group, keV μ -)



MWDC
(from TWIST)



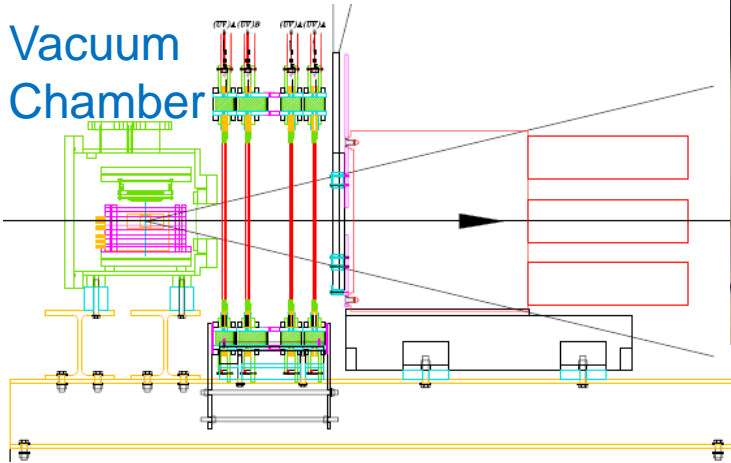
- gas rack
- patch panel
- NIM (trigger)
- visual scalars
- NIM (MWDC HV)
- VME
- NIM (dead)
- PAD (MWDC postamp disc, 2 crates x24x16 ch)
- scintillator HV



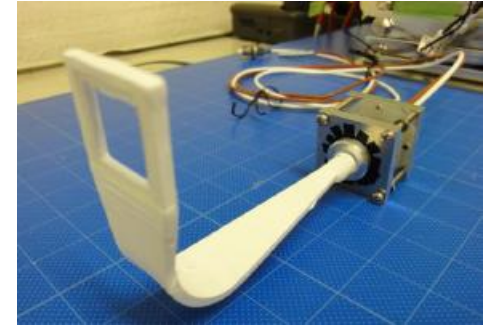
Status of Preparation (2)

at RIKEN /KEK

Vacuum Chamber

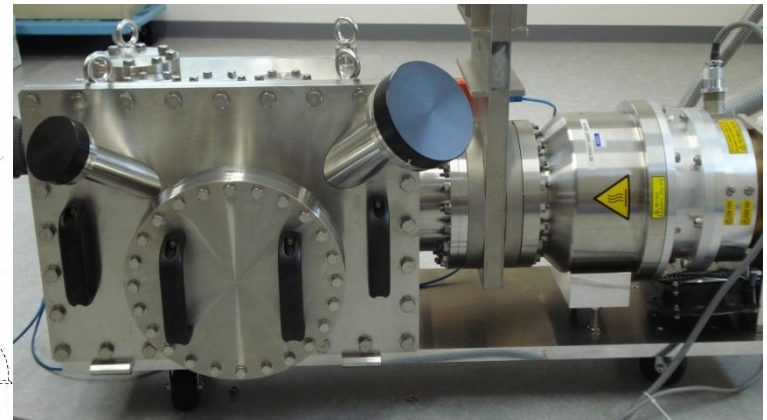
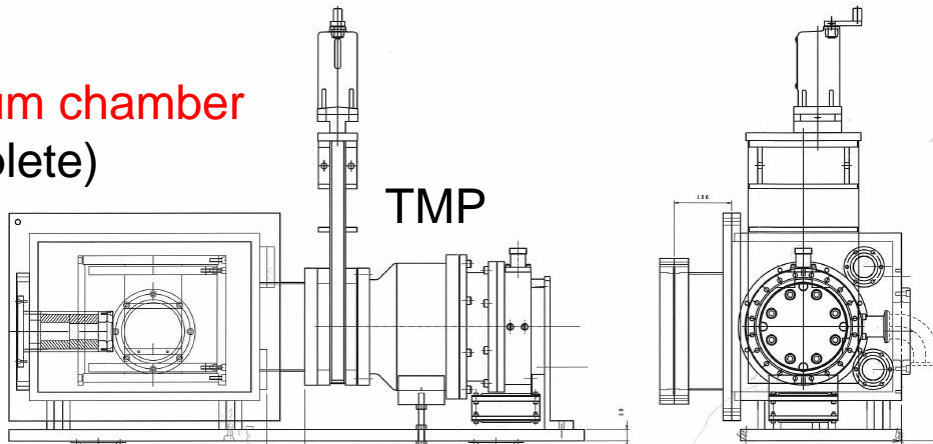


magnet, field cage (ready)



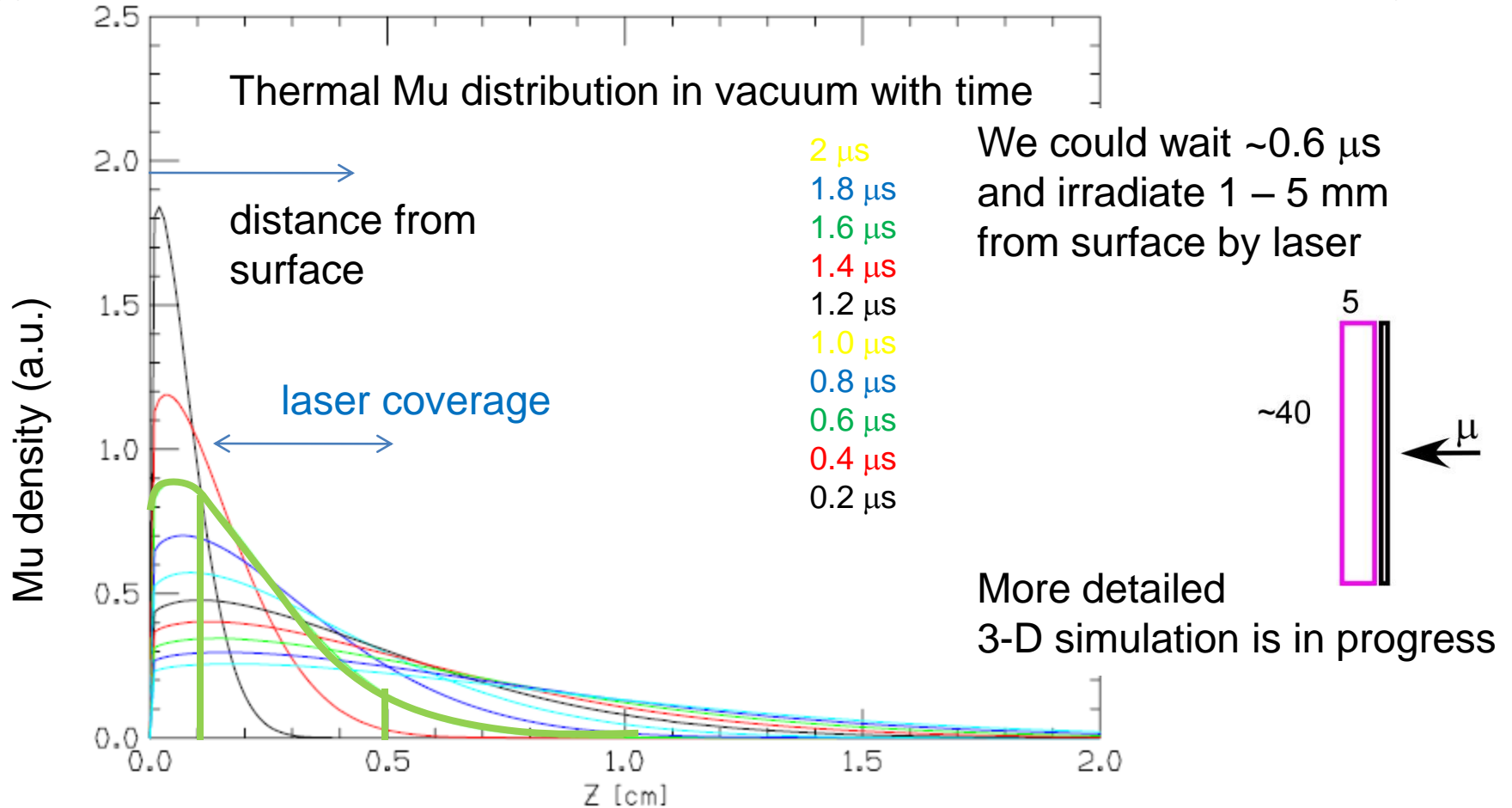
beam counter

Vacuum chamber
(complete)



Laser overlap with muonium

Typical model calculation on **Muonium distribution** in vacuum (model assumption)



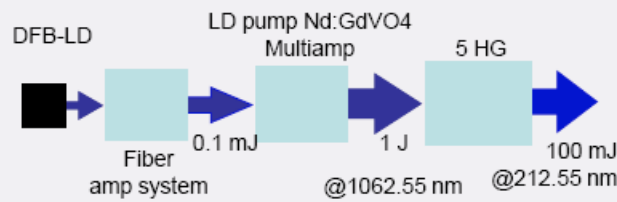
Parameters to describe Mu distribution will be obtained from the measurement
Then, we can design the ionizing laser (timing and laser beam shaping)

Ionizing laser development at RIKEN

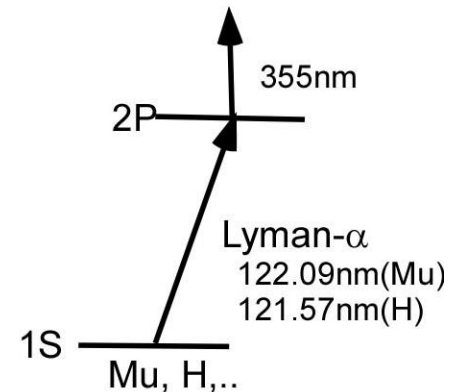
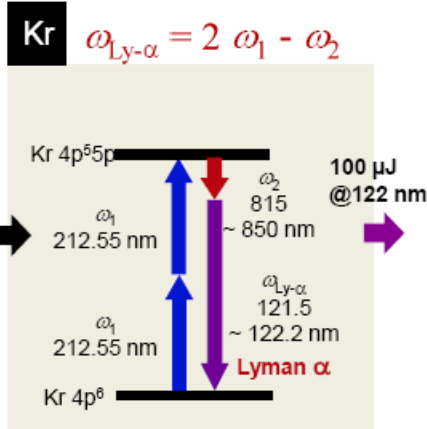
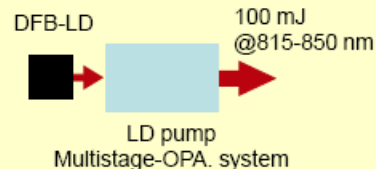
Under development by RIKEN laser group (S. Wada, Nori Saito) and K. Yokoyama
 <= expertise of building stable laser systems, in house technique of special crystal growing, energy compact system, 4 wave mixing simulation



■ Pump laser 1: 2-photon resonance at 212.55 nm



■ Pump laser 2: tunable from 815-850 nm



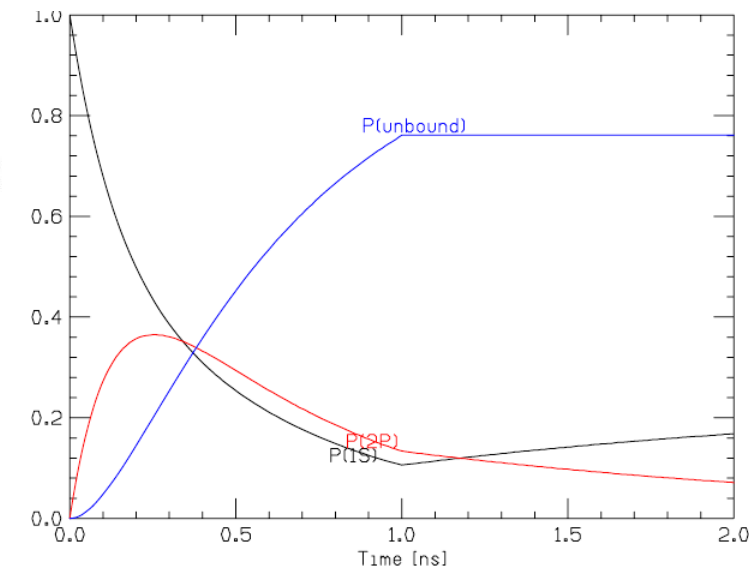
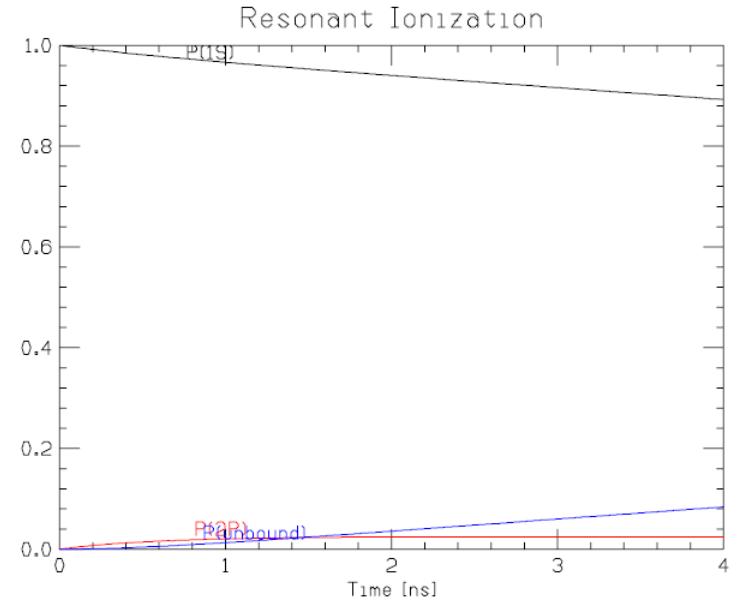
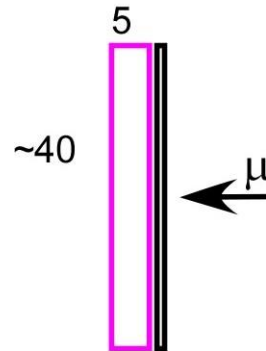
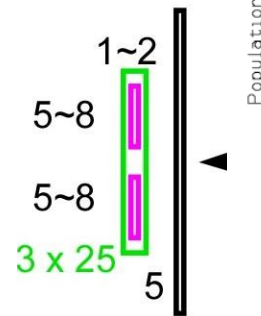
Ionization Process

Estimation of ionizing process versus
laser intensity
based on rate equation & transition rate

Case for $I(\text{Lyman-}\alpha) = 1 \mu\text{J}$,
 $I(355) = 300 \text{ mJ}$
length = 4 ns
ionization 0.11 (??)

Case for $I(\text{Lyman-}\alpha) = 100 \mu\text{J}$
 $I(355) = 300 \text{ mJ}$
length = 1 ns
gives **ionization efficiency = 0.76** after 1 ns

x 7 ionization
x 10 larger area (& higher density)
linear increase
with the expense of larger source size



Acceleration of muons

Acceleration without heating

keep the low transverse momentum spread as low as possible.

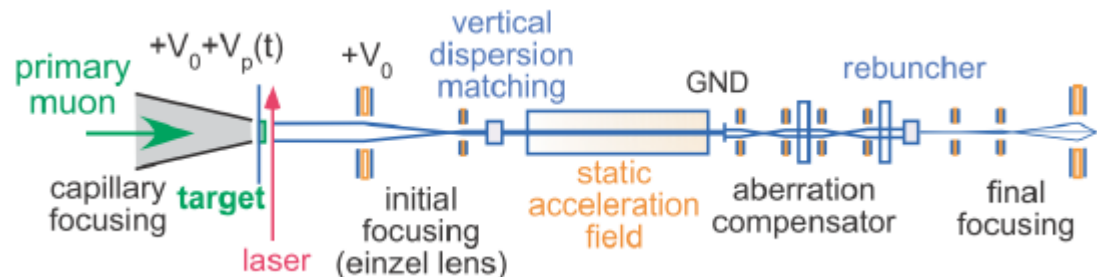
Present scheme (collaboration with linac experts)

Initial acceleration (a few 100keV)

-> low beta linac ($\beta \sim 0.1-0.5$, to 14MeV)

-> high beta linac (up to 300 MeV)

Design of initial acceleration without higher order aberration (by K. Tsukada)
working with electron/ion microscope experts



Initial acceleration with cooling, phase rotation

Various possibilities depending on what we need:

ionizing timing controlled by laser

1) transverse momentum suppression [Iwasaki]

Only muons with a fixed P_T ionized

Doppler shift from resonance for a λ (laser)

By sweeping laser wave length

=> P_T of ionized muons varies with time

by chirped laser

=> dispersion of arriving time vs P_T

=> compensate P_T spread

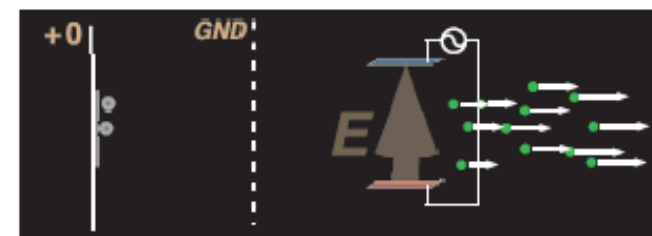
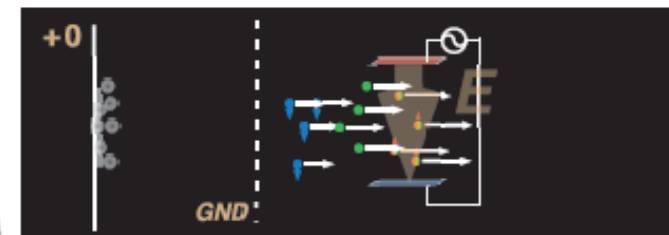
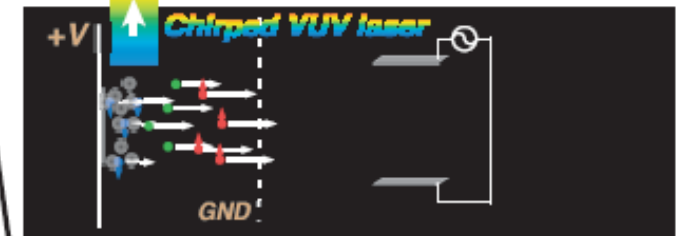
by varying transverse E field

or

2) Making short bunch for injection to linac

3) Reduce energy spread due to ionized position

etc



time

Storage ring and detectors

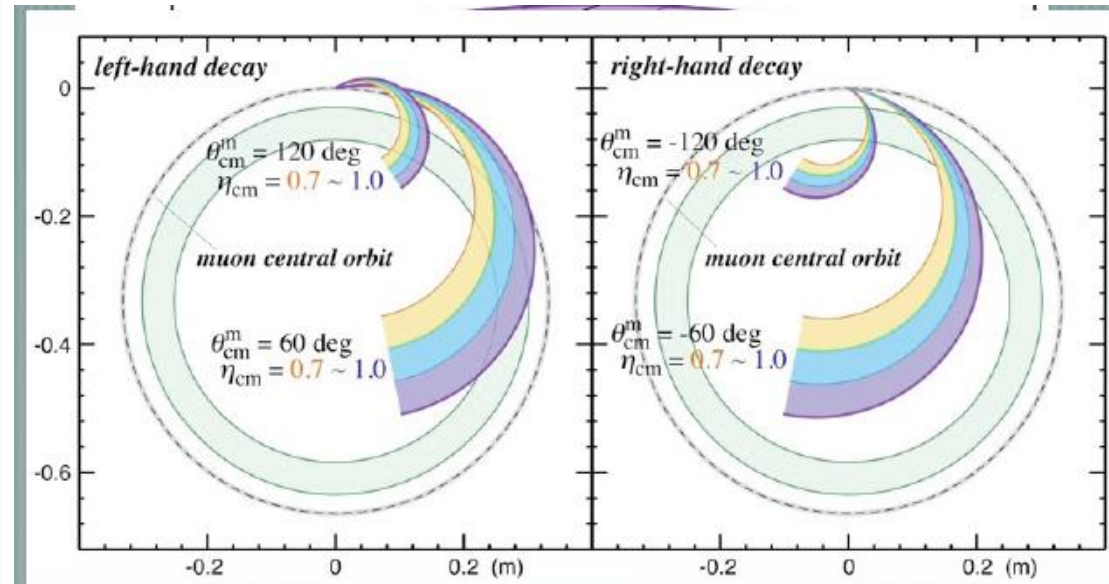
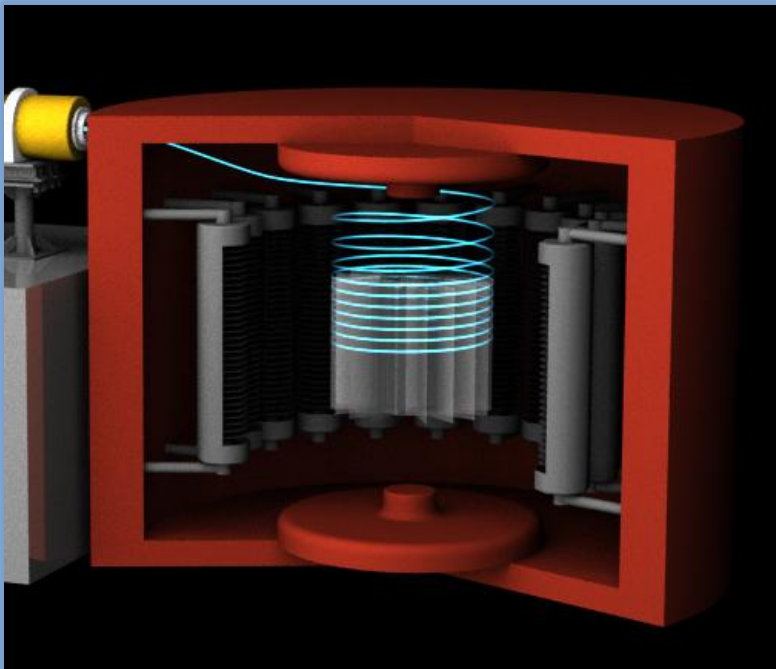
Progress mostly at KEK

Storage ring magnet (based on MRI technology)

Precision field measurement (working on NMR with NIRS)

Beam injection scheme (Iinuma, Nakayama)

Detectors for muon-decay tracking (Mibe, Iinuma)



Summary

A new $g-2$ experiment was proposed at J-PARC

It is based on ultra-cold muon beam

We plan to increase beam intensity to $10^6/s$
and improve beam properties

Room temperature muon source should be developed

Measurement is planned at TRIUMF to study

Intense laser is likely to promise x100 improvement

RIKEN is developing laser and will test at RIKEN-RAL next year.

We are also working on muon acceleration, storage ring etc.

There are still a lot many to do. We welcome your collaboration.

Modeling of Mu diffusion

TRIUMF and PSI model of Mu emission from SiO₂

“effective diffusion rate” for Mu diffusion in target

time for muon to diffuse to surface layer, delayed emission

500 cm²/s (G. Marshall)

1mm thick -> 20 μs ! very slow (10% yield)

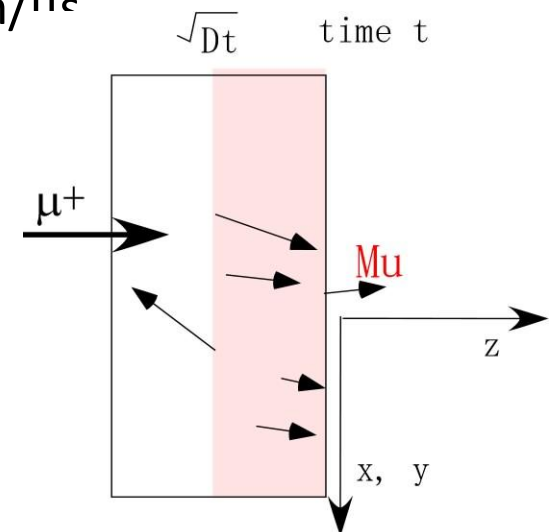
0.1 mm thick -> 200 ns

emitted Mu moves with Boltzman velocity of $\sigma_{vz}=0.5$ cm/μs

z distribution is Gaussian with $\sigma_z=0.5$ cm after 1μs,

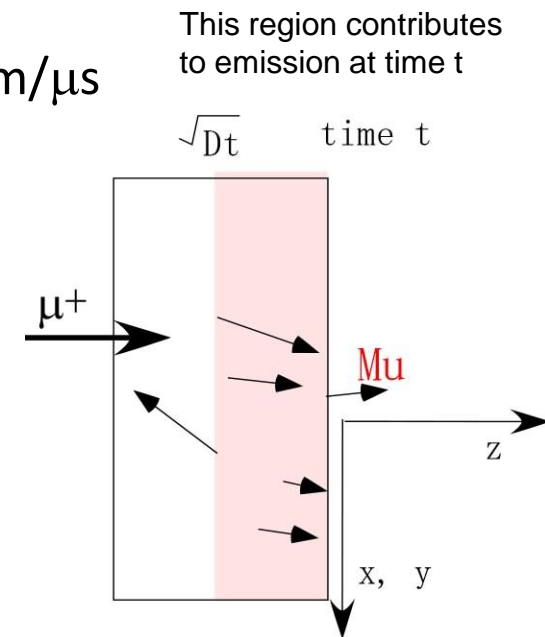
Mu spreads in region $z = 0 \sim 5$ mm

Mu distribution is convolution of these two



Laser overlap with Mu: Modeling of Mu emission

- TRIUMF and PSI model of Mu emission from SiO₂
- “effective diffusion rate” D_2 is one of the parameters
 - time for muon to diffuse to surface layer, delayed emission
 - 500 cm²/s (G. Marshall)
 - 1mm thick -> 20 μ s ! very slow (10% yield)
 - 0.1 mm thick -> 200 ns
- emitted Mu moves with Boltzman velocity of $\sigma_{vz}=0.5$ cm/ μ s
 - z distribution is Gaussian with $\sigma_z=0.5$ cm after 1 μ s,
 - Mu spreads in region $z = 0 \sim 5$ mm
- with this diffusion model and uniform muon stopping, muonium in vacuum increase with $(D_2t)^{1/2}$ (if ignoring muon decay)
 - emission rate is its derivative $(D_2/t)^{1/2}$
- Mu distribution is convolution of these two
 - adding up Gaussian of different width ($\sigma_z(t-t_e) = 0.5(t-t_e)$ cm) with weight $t_e^{-1/2}$



Keys for intense cold muon

1. Target materials

Muonium measurement at TRIUMF (June and Nov 2010)

2. Intense Lyman- α laser

1+2 Combined test at RIKEN-RAL (March 2011-)

3. Initial acceleration scheme

1+2+3 Combined measurement at RIKEN-RAL

4. Highest intensity muon channel at J-PARC (Miyake, Ikedo)

1+2+3+4 Realization of cold muon source for g-2 at J-PARC

Hints for high Mu yield

While the understanding is far from complete, material with **large surface area** seems essential

1. diffuse out of muon from substance

fine particle (size a), diffusion in bulk (D_{bulk})

$$\text{yield} \sim D_{\text{bulk}}^{0.5} / a$$

2. Mu diffusion in void channels

target thickness (b), diffusion through voids (D_{void}),

$$\text{yield} \sim D_{\text{void}}^{0.5} / b$$

large mean free path (l) & interconnecting void channels

- high void/material ratio

free interacting gas model ($D = 1/l \sim \rho^{-1/3}$)

whereas **high muon stopping density** ($\sim \rho$)

